

Introduction to X-ray production

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Outline

1. Mechanisms for X-ray production

Charge acceleration: bremsstrahlung

Electronic quantum transitions

2. X-ray tubes for X-ray diffraction measurements

3. Principles of synchrotron radiation

Synchrotron Radiation:

What is it?

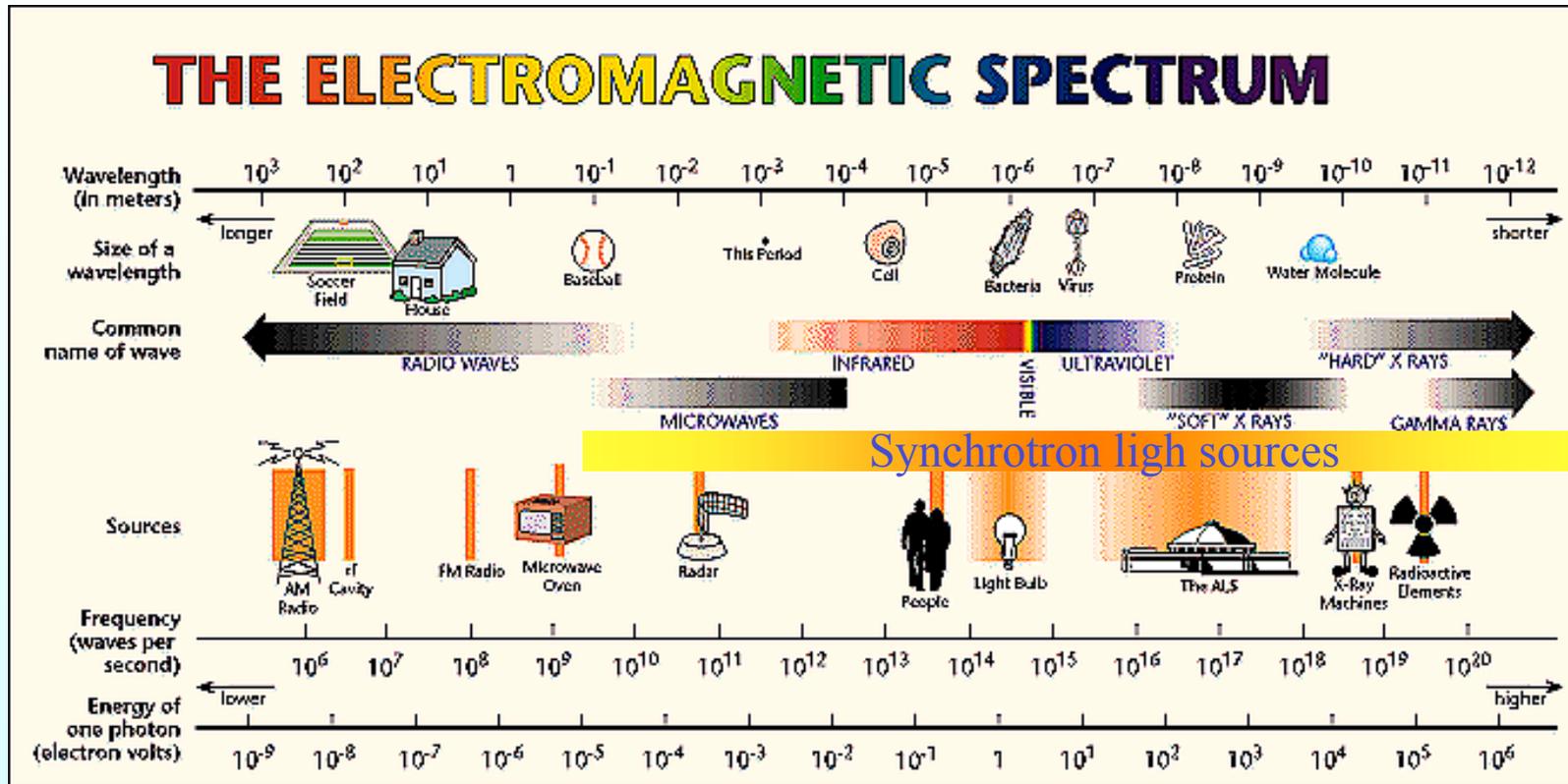
How is it produced?

Which are their properties?

... which the main uses?



Electromagnetic Radiation and Structure of matter



The shorter the wavelength, the greater the resolution for observing small object

Synchrotron radiation sources span wide regions of the electromagnetic spectrum



Who are the responsables of light emission?

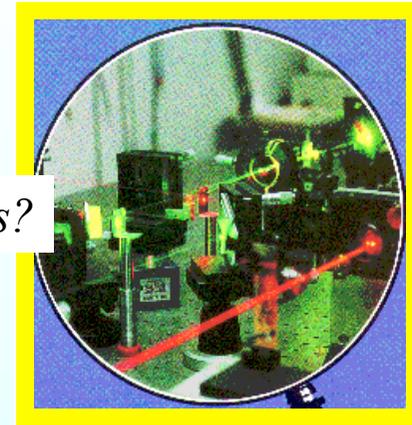
From a candle?



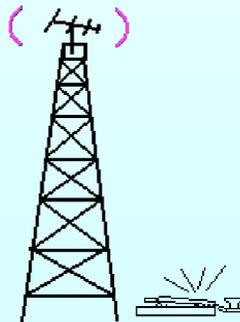
da una lamfrom a lamppada?



From lasers?



By a broadcasting antenna?



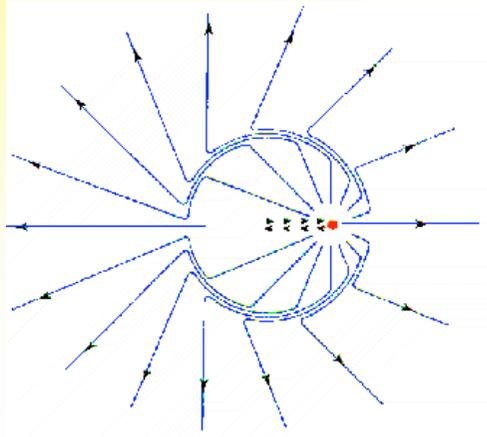
The amin responsible are the electrons



Radiation production mechanisms

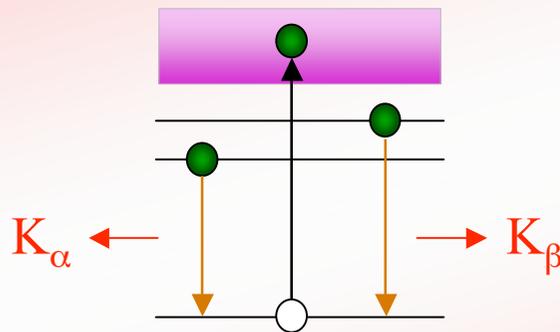
There are two ways to produce synchrotron radiation:

Classical mechanism: acceleration of charged particle (for instance, electrons and positrons)



- Bremsstrahlung: deceleration of high energy electrons in a metal
- Synchrotron radiation emitted by relativistic charged particles in particle accelerators
- Cosmic synchrotron radiation

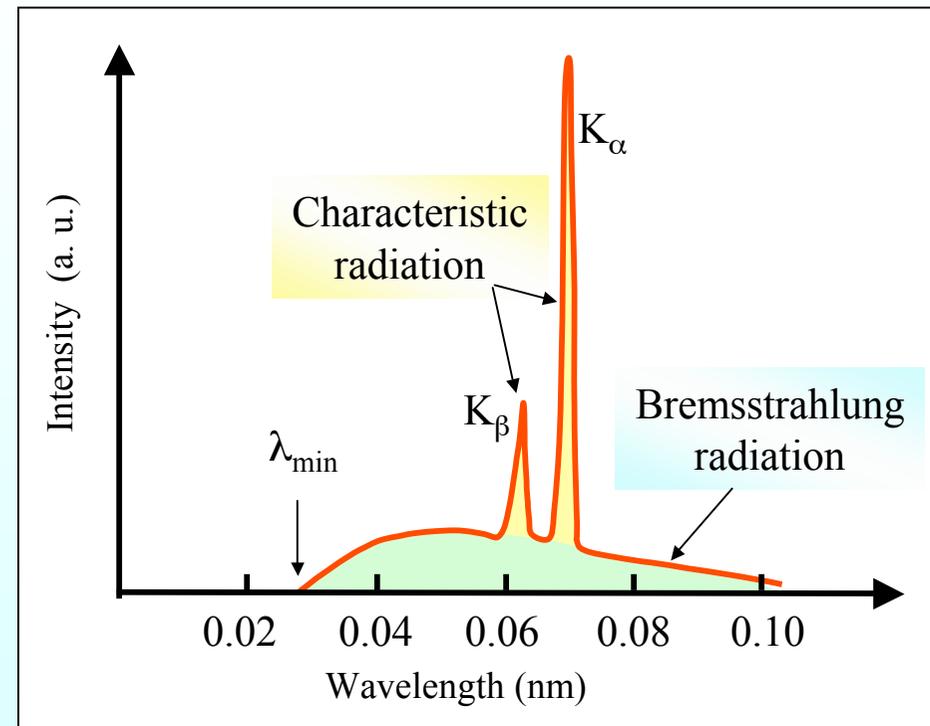
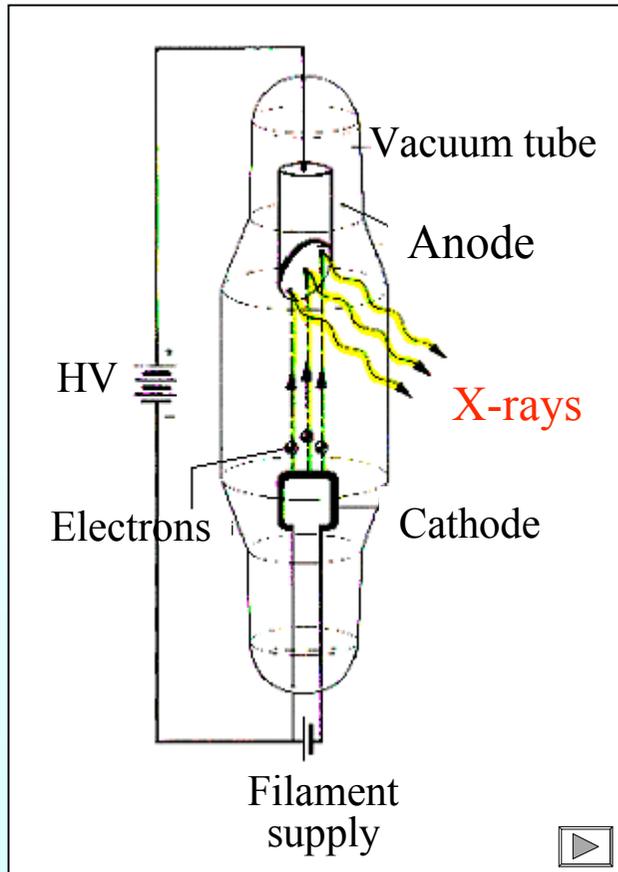
Quantum mechanism: transitions of electrons from outer to inner empty energy levels



- Emission lines
- Characteristic radiation



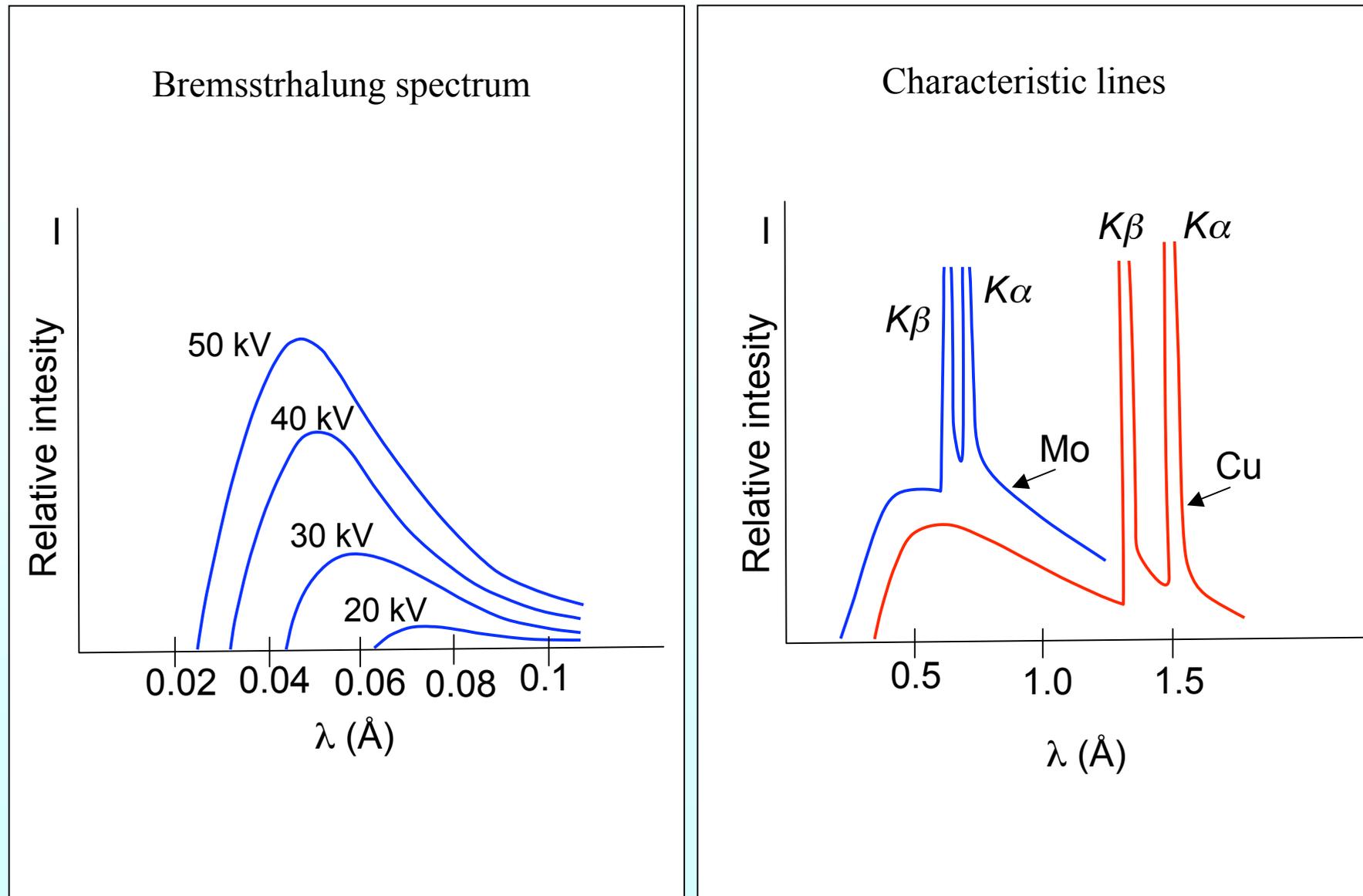
X ray production by tubes



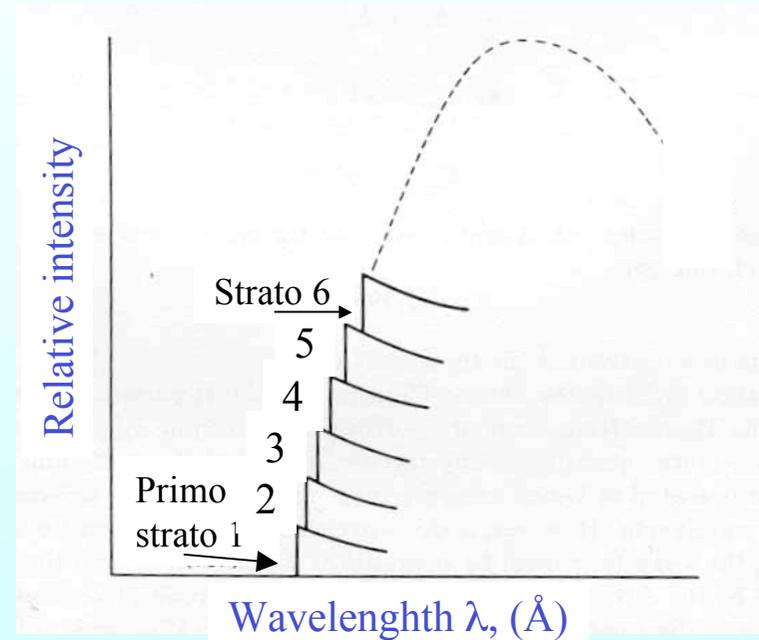
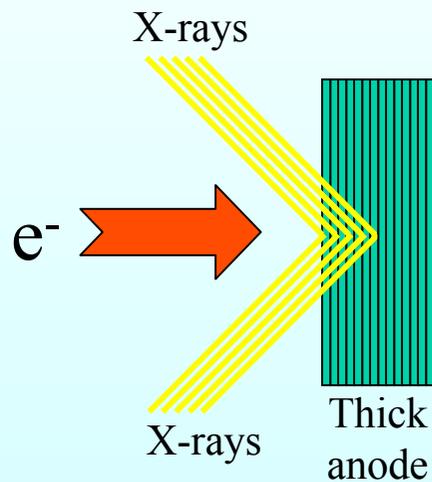
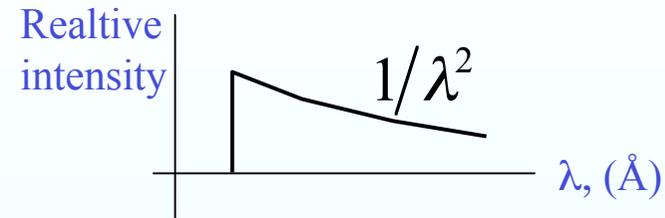
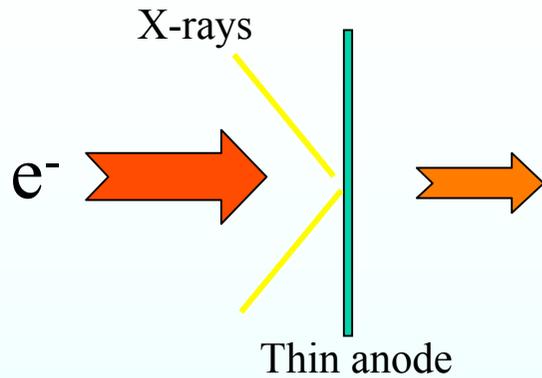
The spectrum from an X ray tube has discrete fluorescent lines superimposed on the continuous bremsstrahlung radiation



Spectra of different anodes



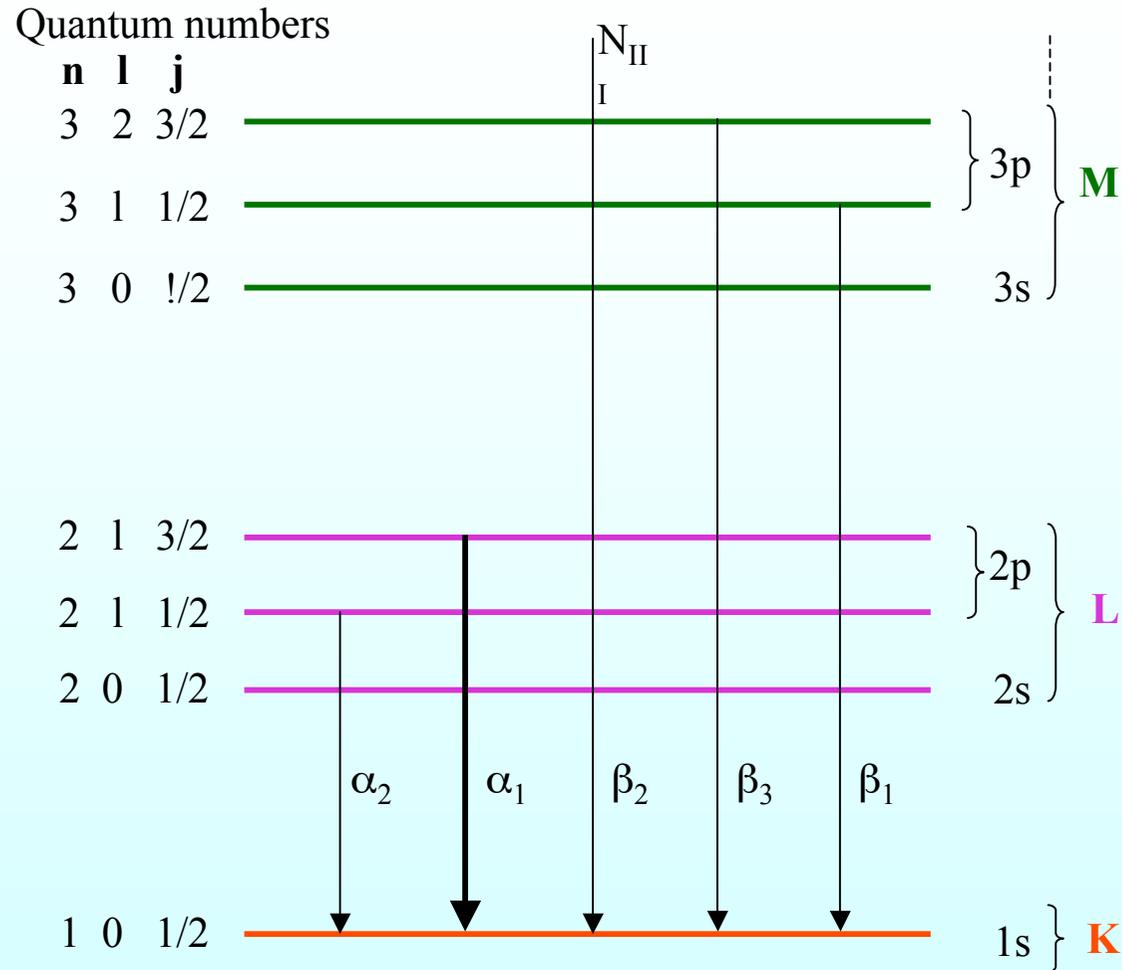
Distribuzione spettrale



The continuous spectrum emitted by a thick anode can be considered as the summation of spectra emitted by thin layers of the anode



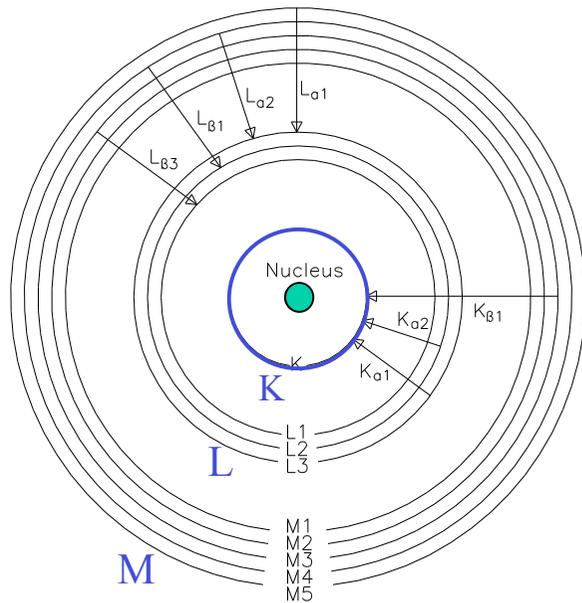
Electronic transitions and K emission lines



Simplified diagram of transitions from energy states characteristic of the K emission line series



Characteristic spectrum



It consists of series of discrete lines whose energy is equal to the energy difference of two atomic levels.

Each element has its own characteristic spectrum

Line emission denomination

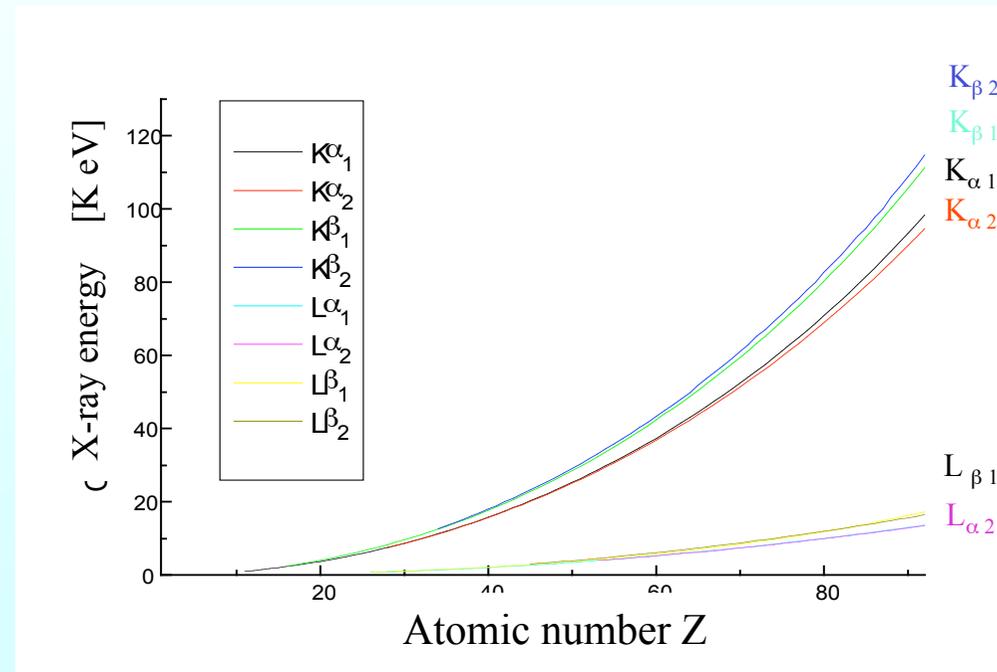
Siegbahn	IUPAC	Siegbahn	IUPAC
K _γ ₁	K-L3	L _γ ₁	L3-M5
K _γ ₂	K-L2	L _γ ₂	L3-M4
K _β ₁	K-M3	L _β ₁	L2-M4
K _β ₂	K-N2,N3	L _β ₂	L3-N5
K _β ₃	K-M2	L _β ₃	L1-M3
		L _β ₄	L1-M2



Moseley law

Relationship between the atomic number of an element and the energy of its spectral emission lines

$$E(Z) = k_j (Z - \sigma_j)^2$$

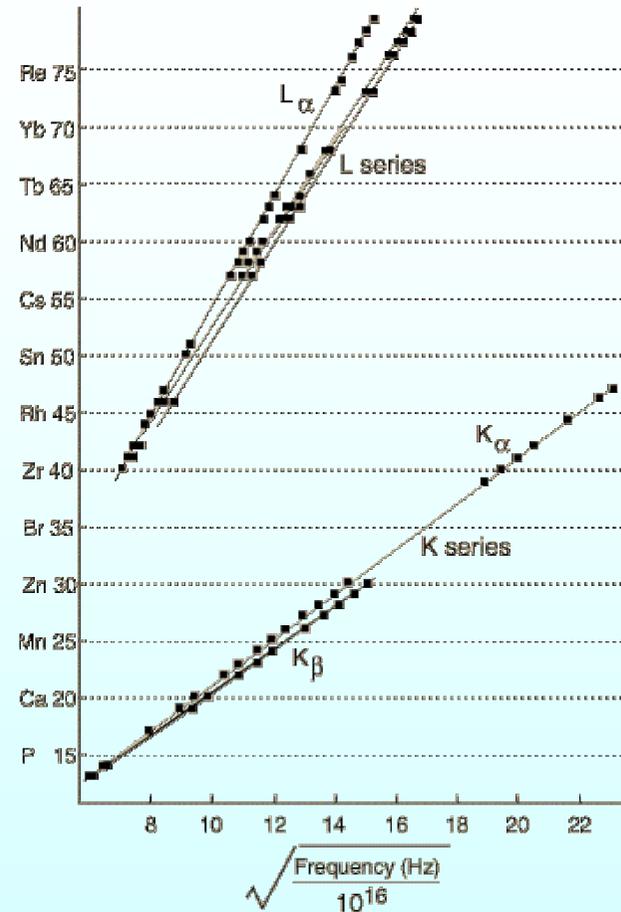


In terms of wavelength, the previous equation is:

$$\lambda \propto \frac{1}{Z^2}$$



Moseley Plot of Characteristic X-Rays



Adapted from Moseley's original data (H. G. J. Moseley, Philos. Mag. (6) 27:703, 1914)

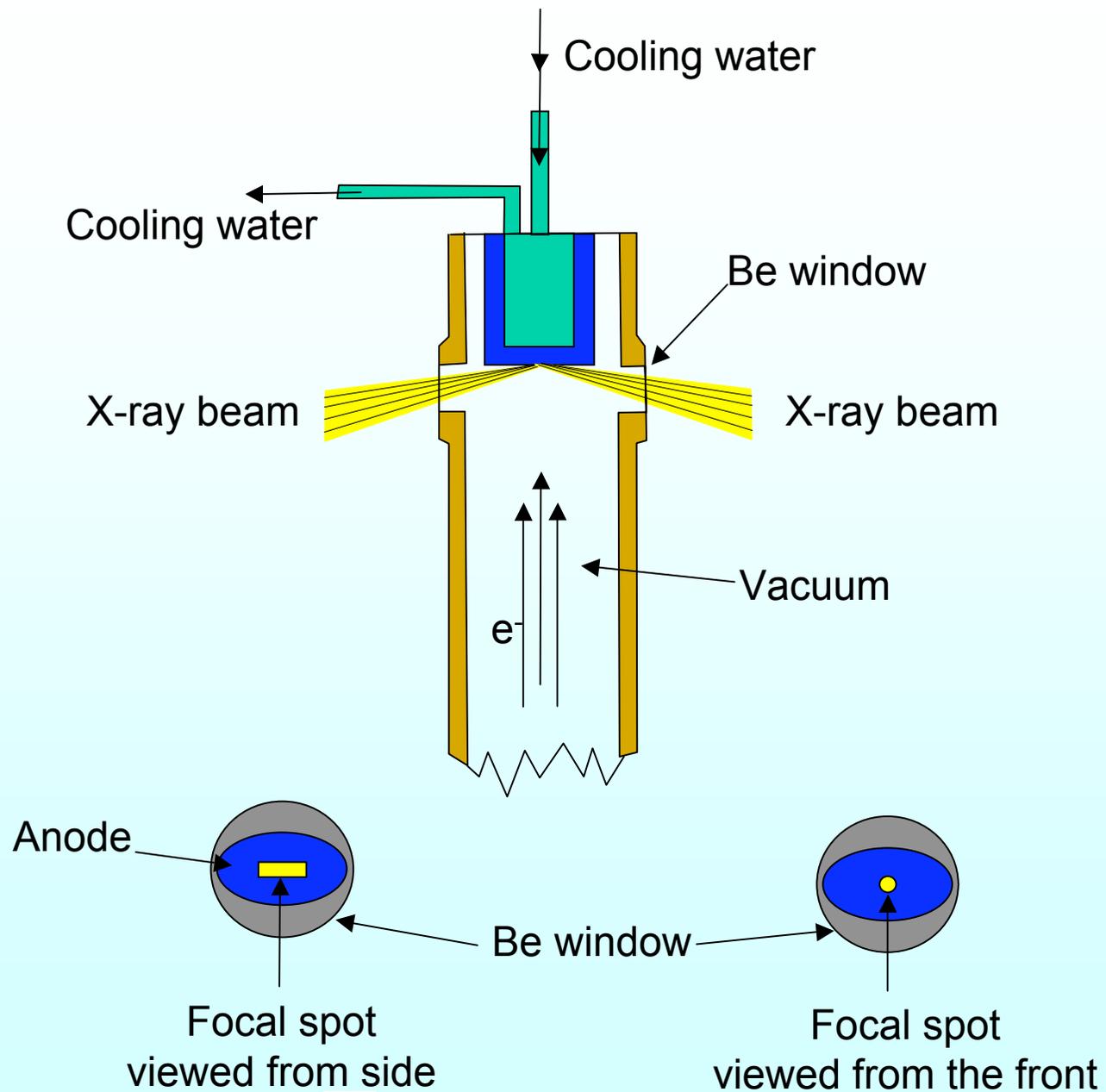
$$h\nu_{K\alpha} = 13.6\text{eV} (Z-1)^2 \left[\frac{1}{1^2} - \frac{1}{2^2} \right] = \frac{3}{4} 13.6 (Z-1)^2 \text{ eV}$$



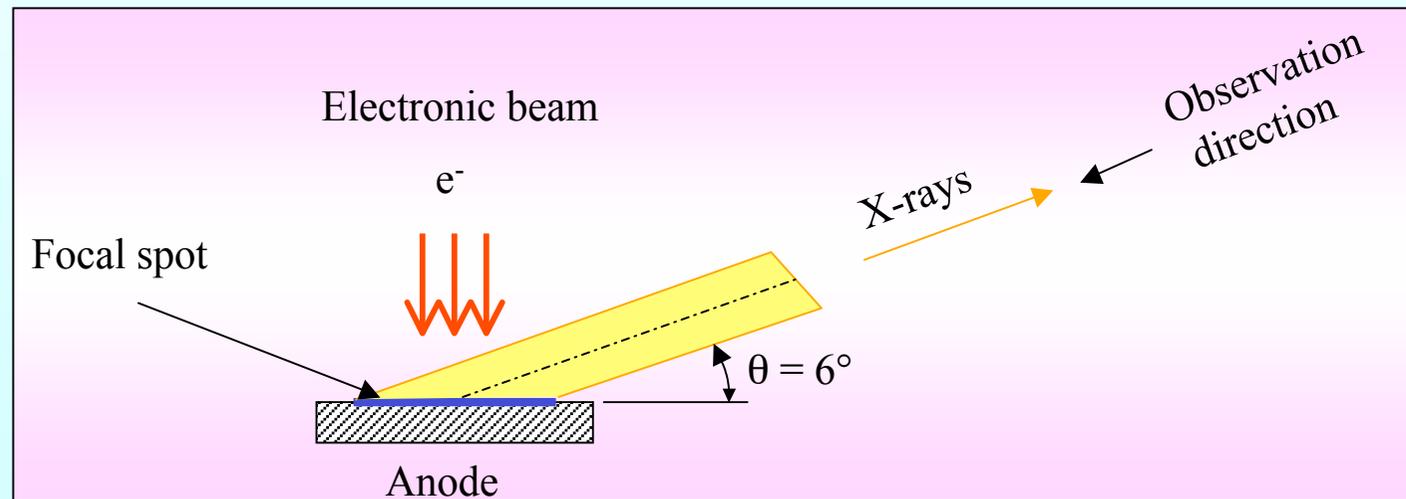
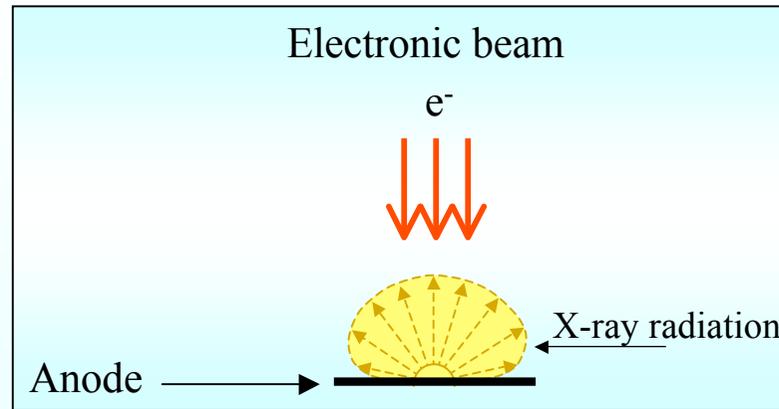
Target materials and associated constants

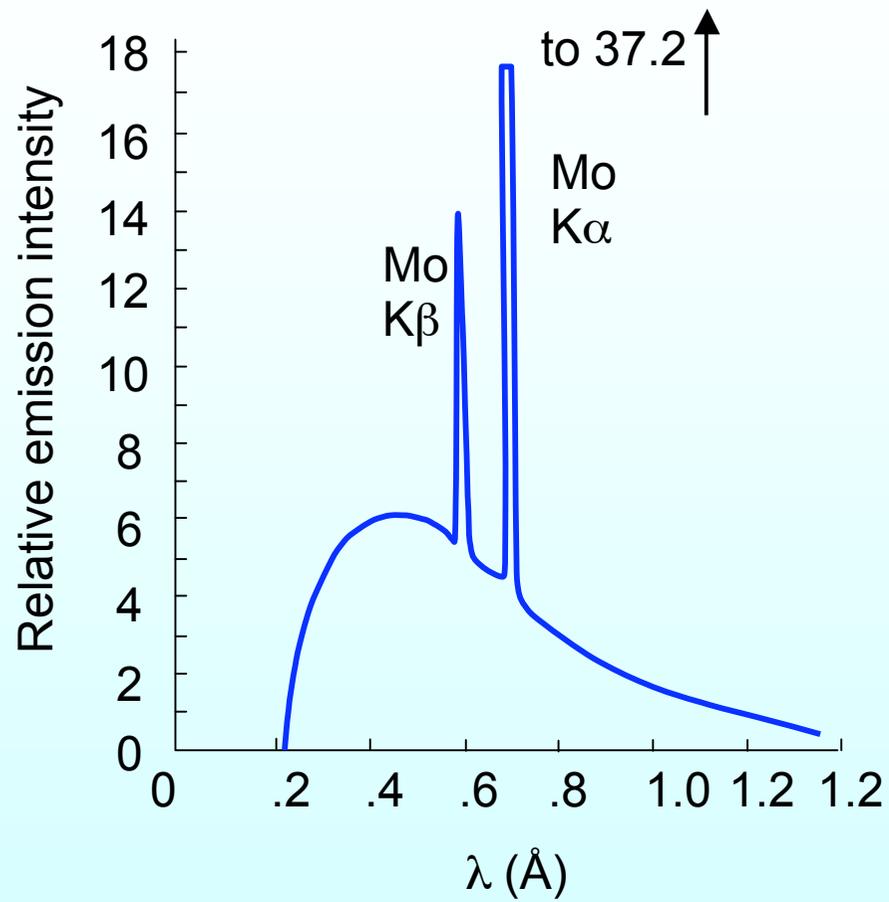
	Cr	Fe	Cu	Mo
Z	24	26	29	42
$k_{\alpha 1}$, (Å)	2.2896	1.9360	1.5405	0.70926
$k_{\alpha 2}$, (Å)	2.2935	1.9399	1.5443	0.71354
$K_{\alpha 1-2}$, (Å)	2.2909	1.9373	1.5418	0.71069
$k_{\beta 1}$, (Å)	2.0848	1.7565 [†]	1.3922	0.63225
β filter	V	Mn	Ni	Nb
α filter	Ti	Cr	Co	Y

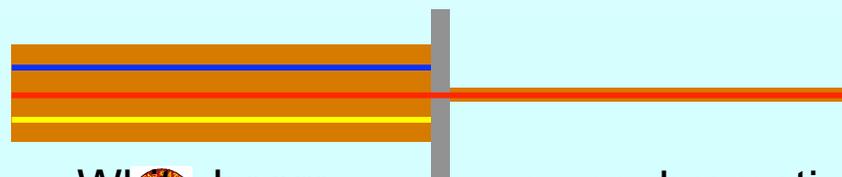
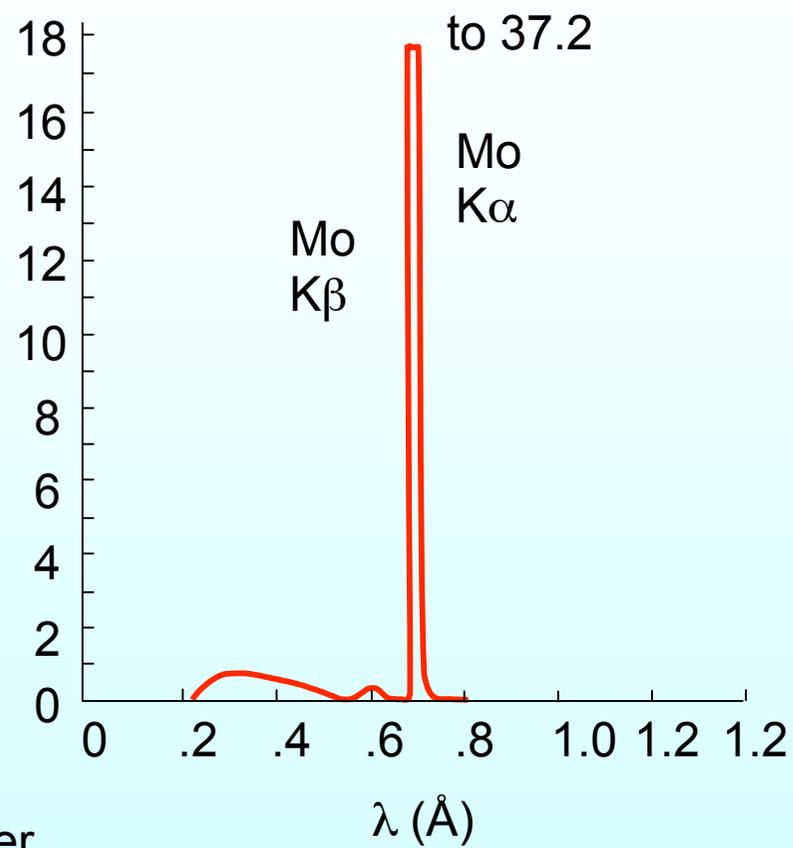
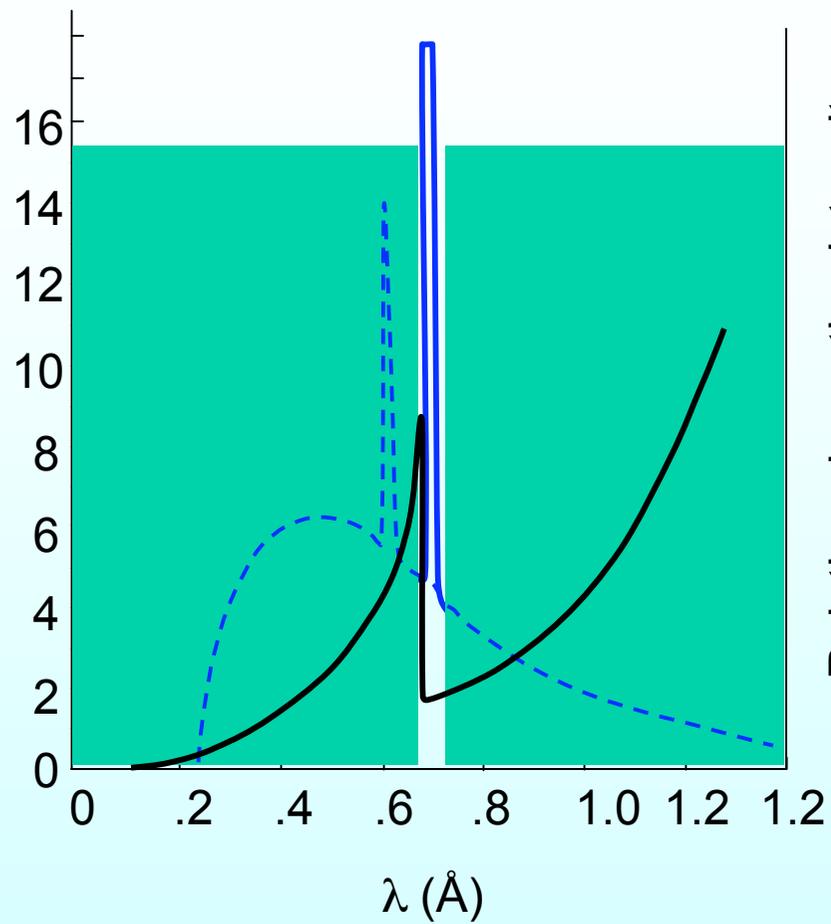




Angular distribution of the radiation emitted by an X-ray tube







White beam

monochromatized beam



Giuseppe Dalba, University of Trento, Italy

Charged particles moving in circular motion radiate

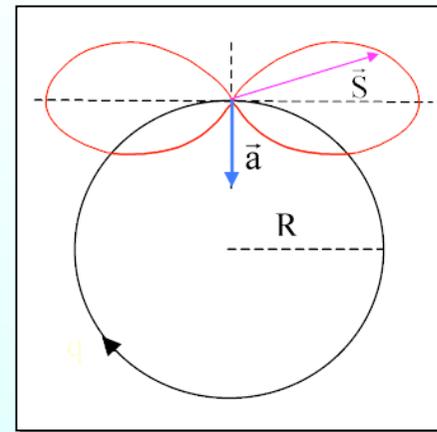
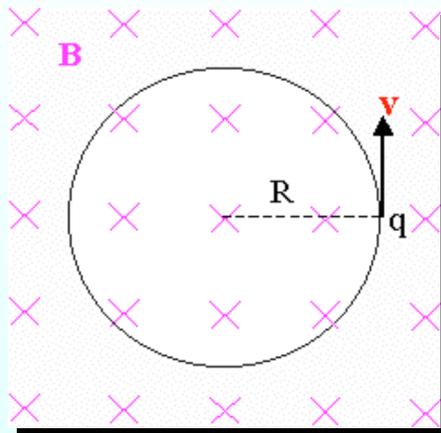
Larmor Formula

$$P = \frac{q^2 a^2}{6\pi\epsilon_0 c^3}$$

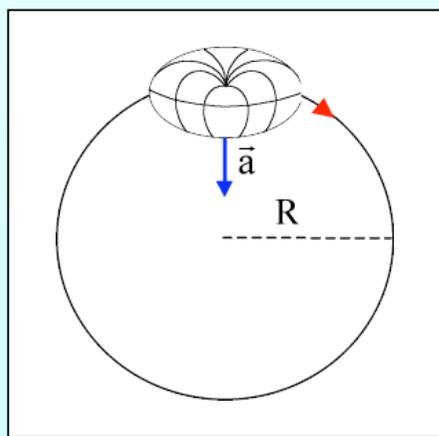
P = Electromagnetic power

q = charge

a = centripetal acceleration



S = Pointing vector

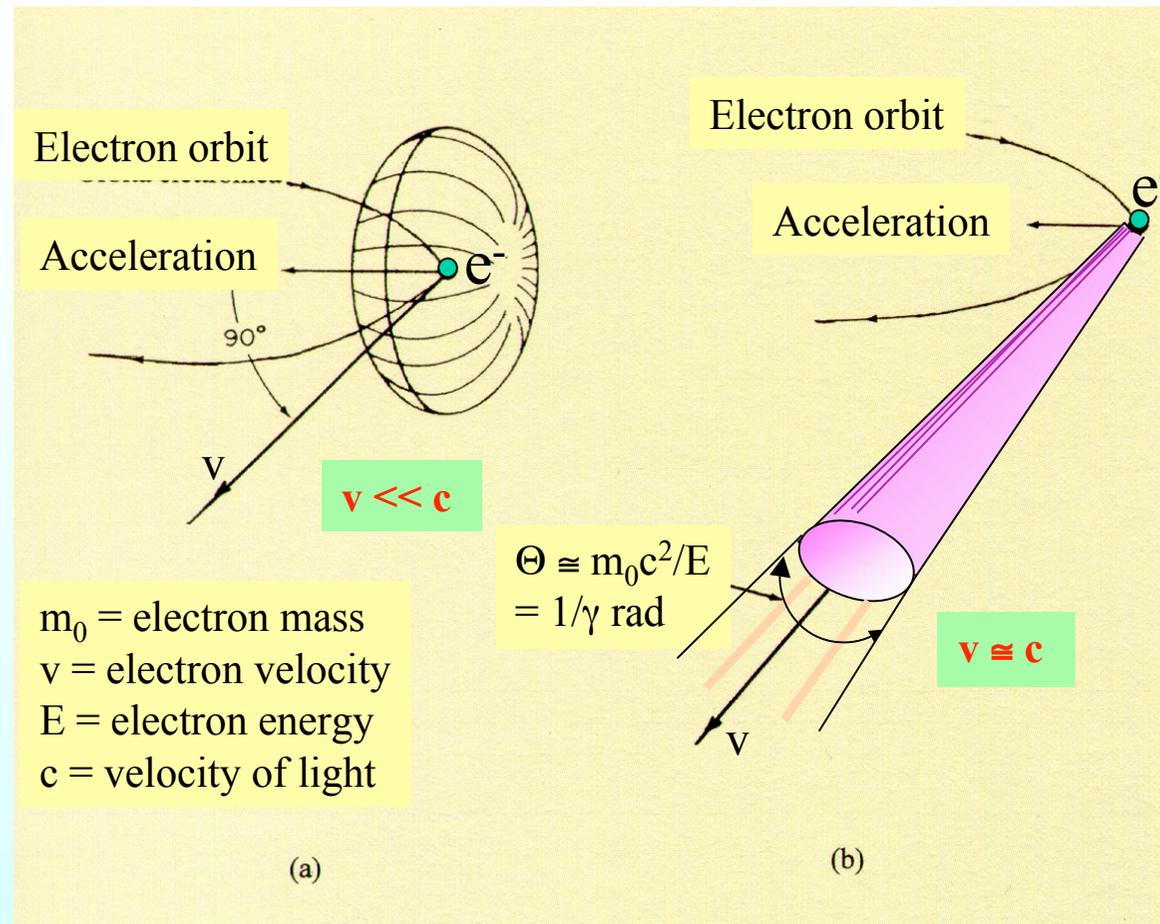


$$v \ll c$$

The radiation angular distribution of non-relativistic electrons has the shape of a tire orbiting at the same velocity of the electron bunch



Synchrotron radiation angular distribution

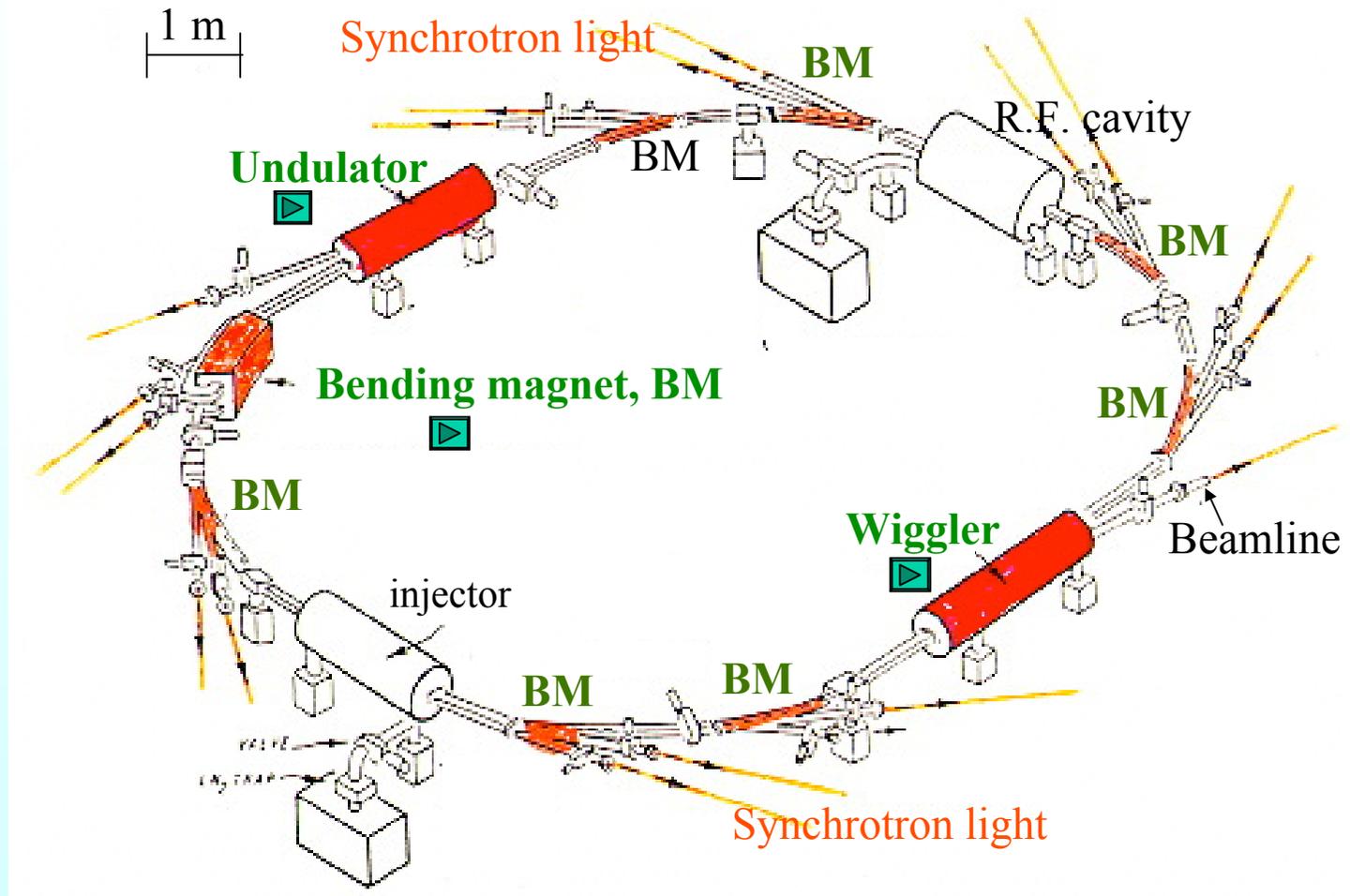


Top view

Radiation angular distribution (a) electrons travelling at low speed
 (b) electrons travelling at relativistic speed ($\gamma = (1-v^2/c^2)^{-1/2} \approx 10000$ at ESRF)



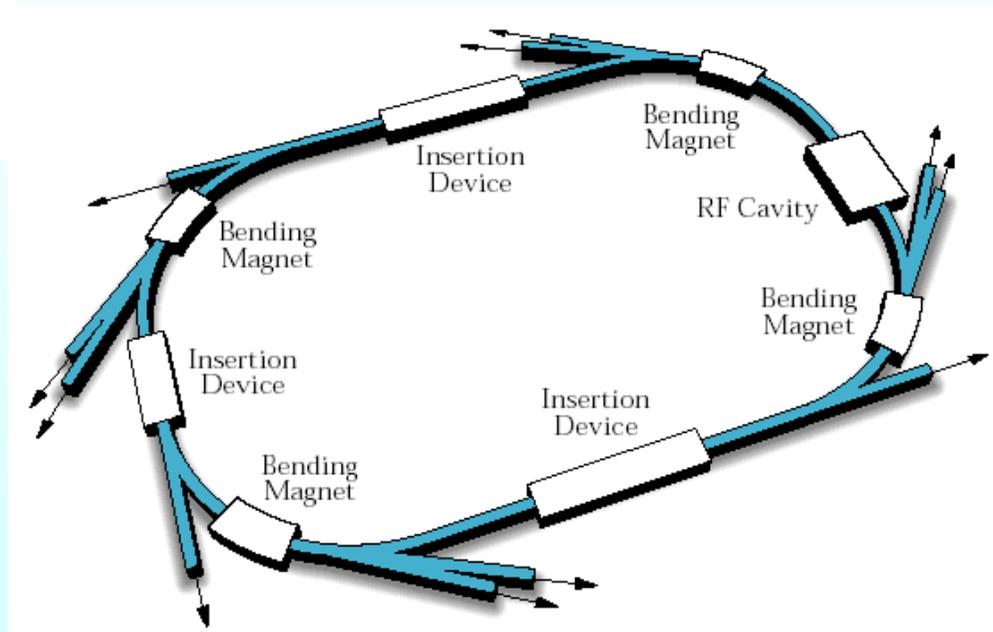
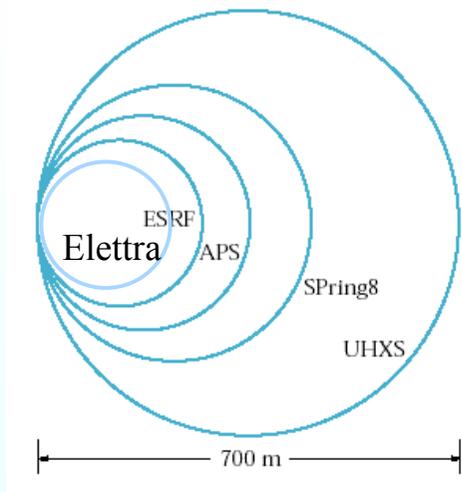
Synchrotron light from a storage ring



 Animation

 Three types of magnetic systems



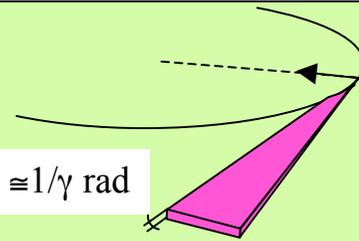


Properties of synchrotron radiation

High collimation



$$\Theta \cong 1/\gamma \text{ rad}$$



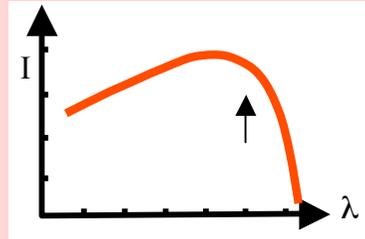
Bending Magnets

Wigglers

Undulators

High flux

Wide spectrum

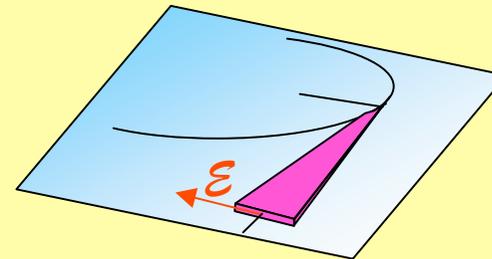


BM

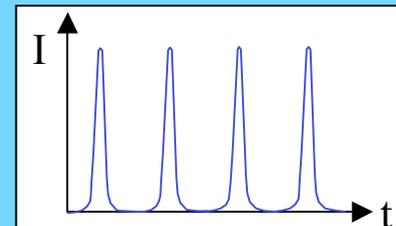
ID

Brilliance

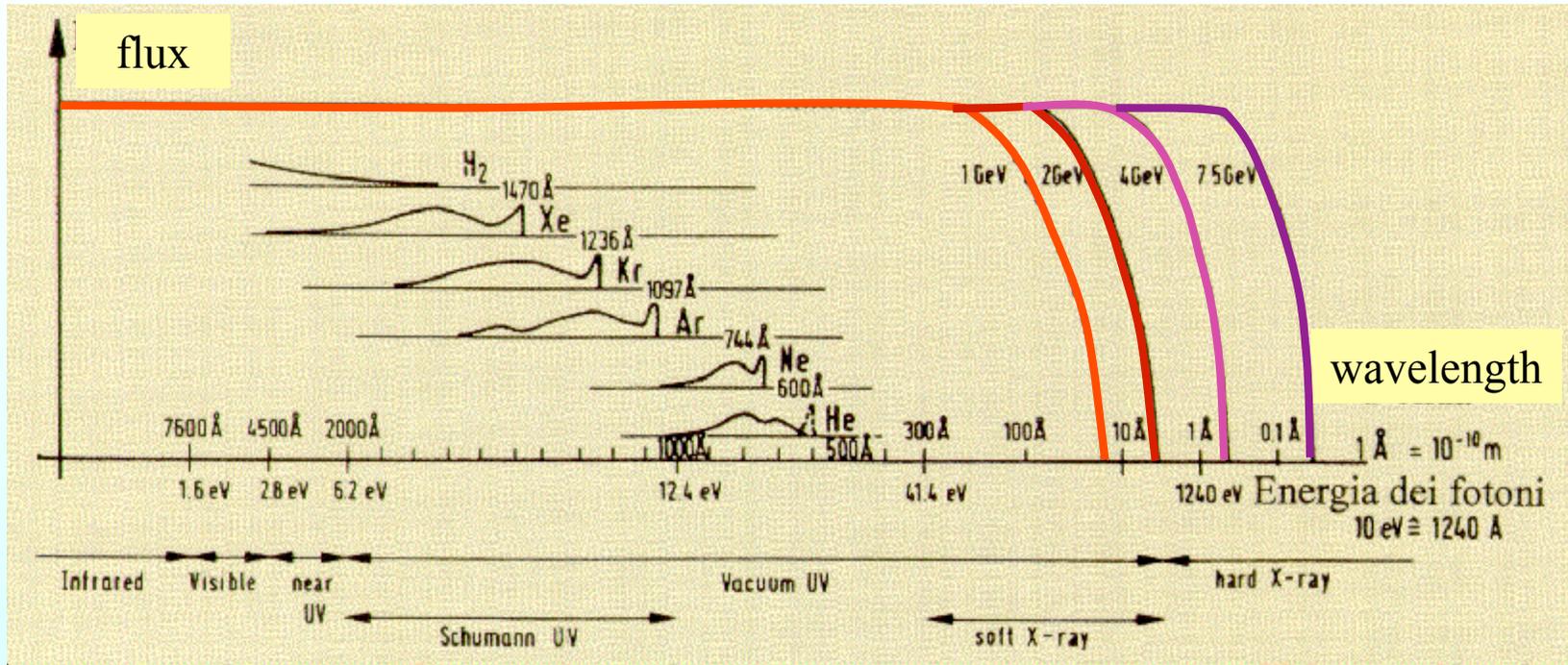
Polarization



Temporal structure



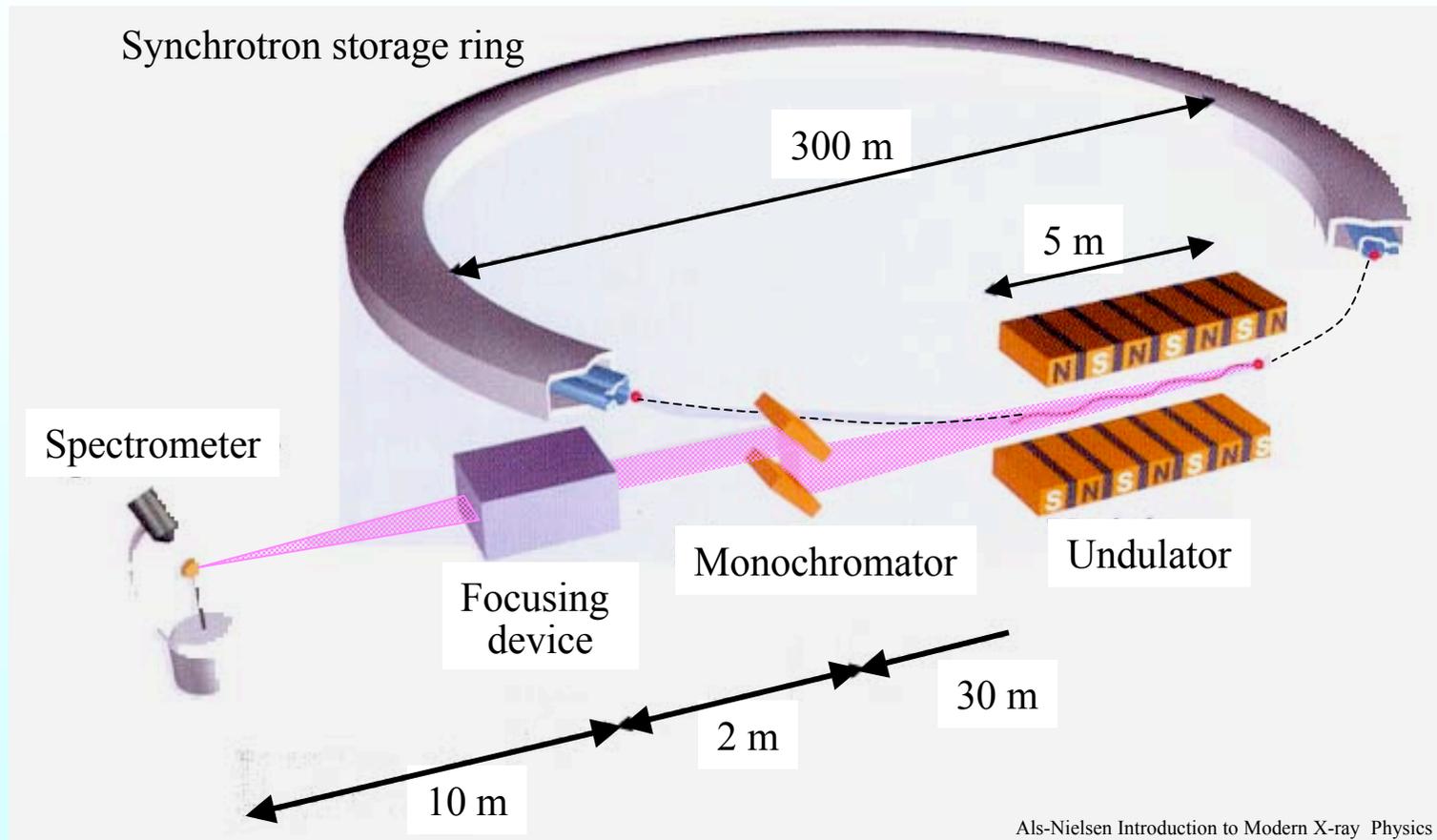
Spectral distributions of different sources



Intensity and spectral range of synchrotron radiation sources are several order of magnitude greater than those of rare gas discharge lamps.



From the magnetic device to the experimental station



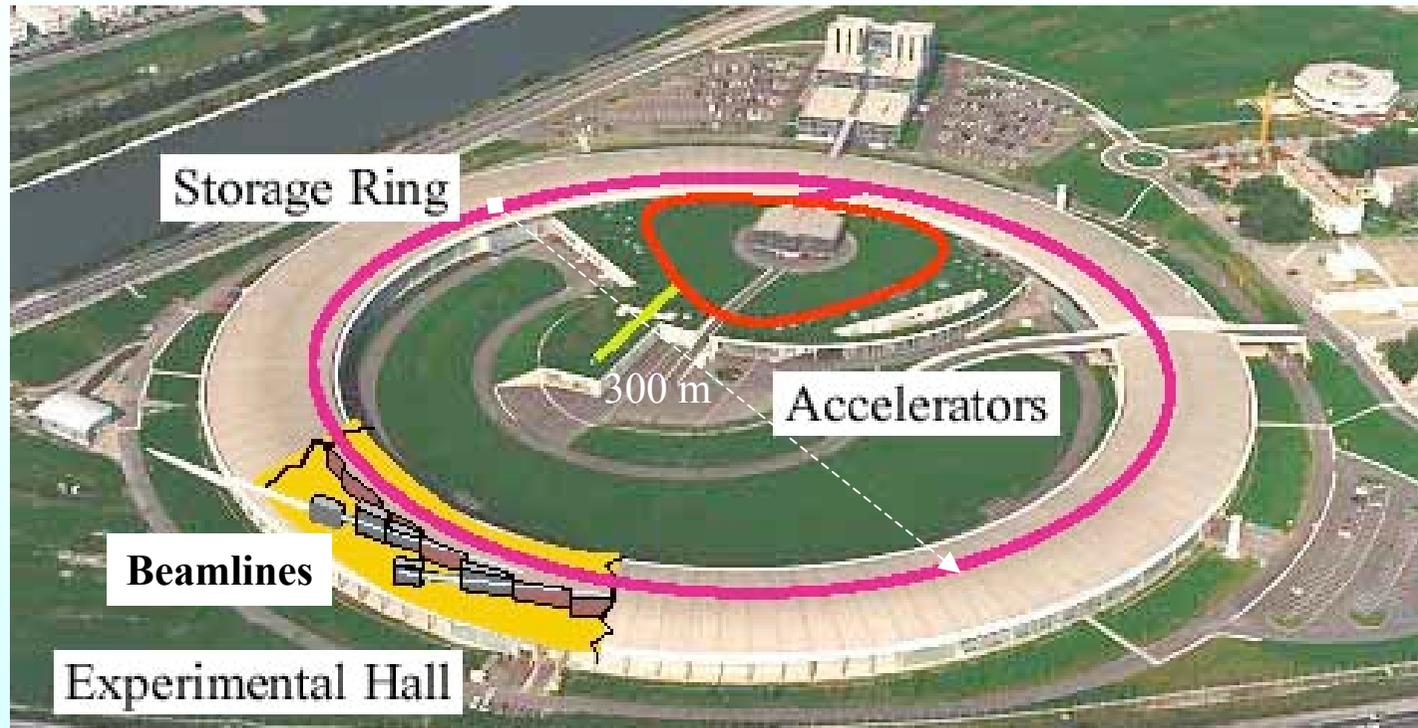
ESRF - Grenoble



The greatest concentration of laboratories in matter Physics in Europe



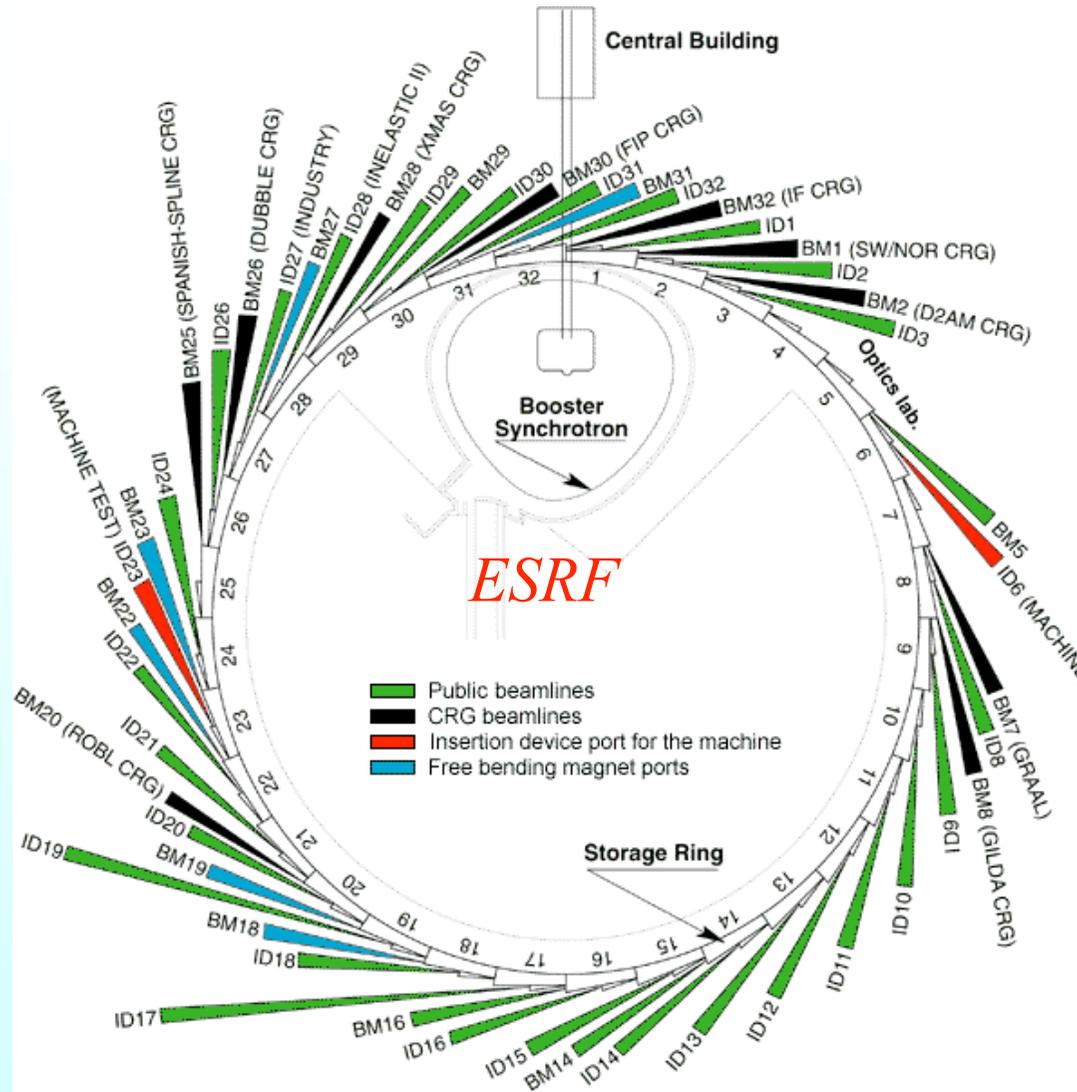
The Grenoble machine



The European Synchrotron Radiation Facility (ESRF)

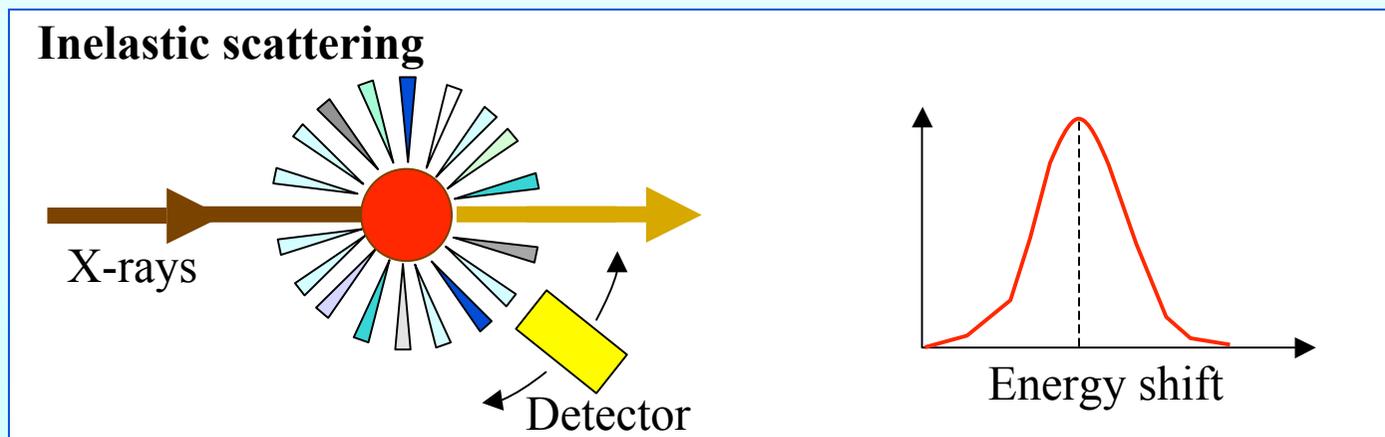
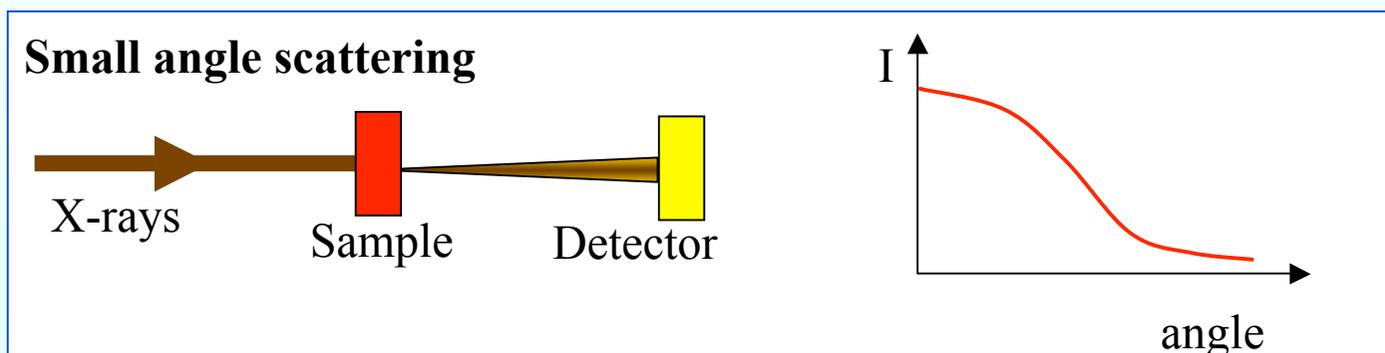
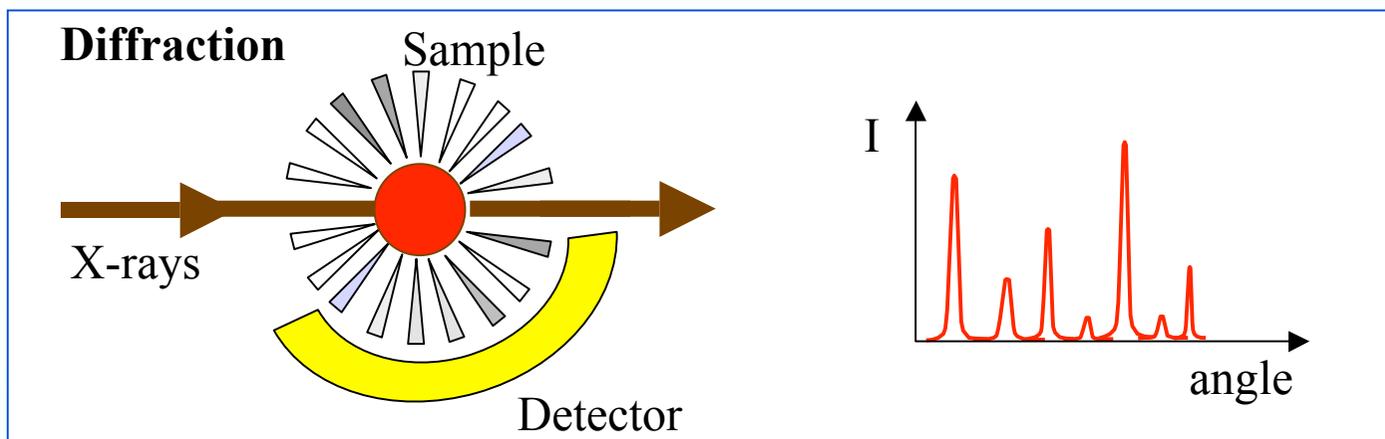


ESRF beamlines

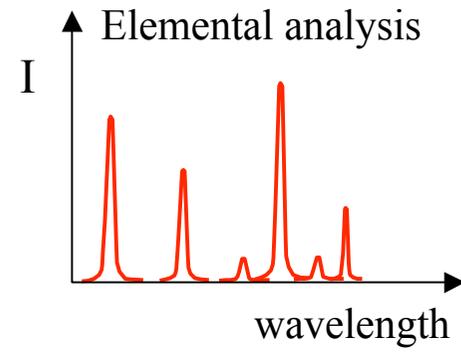
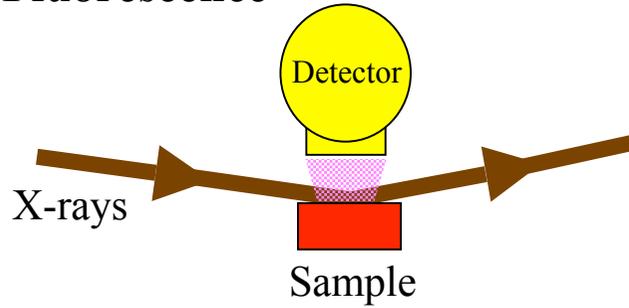


Each beamline hosts one or more specialized experimental stations

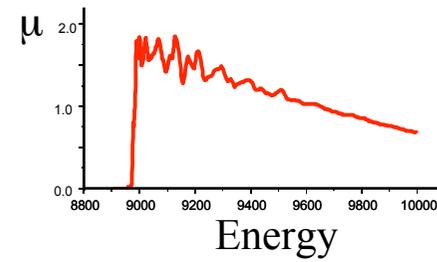
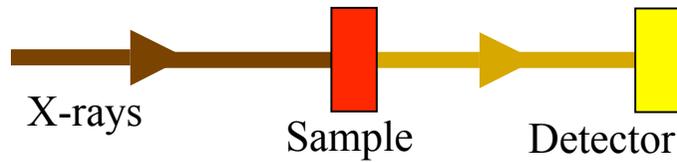




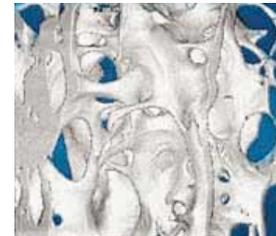
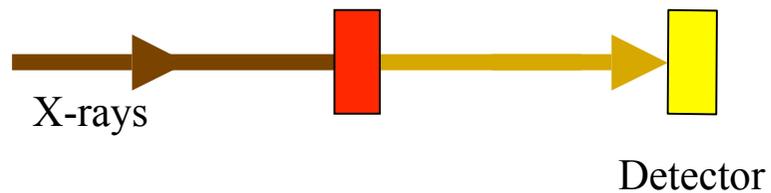
Fluorescence



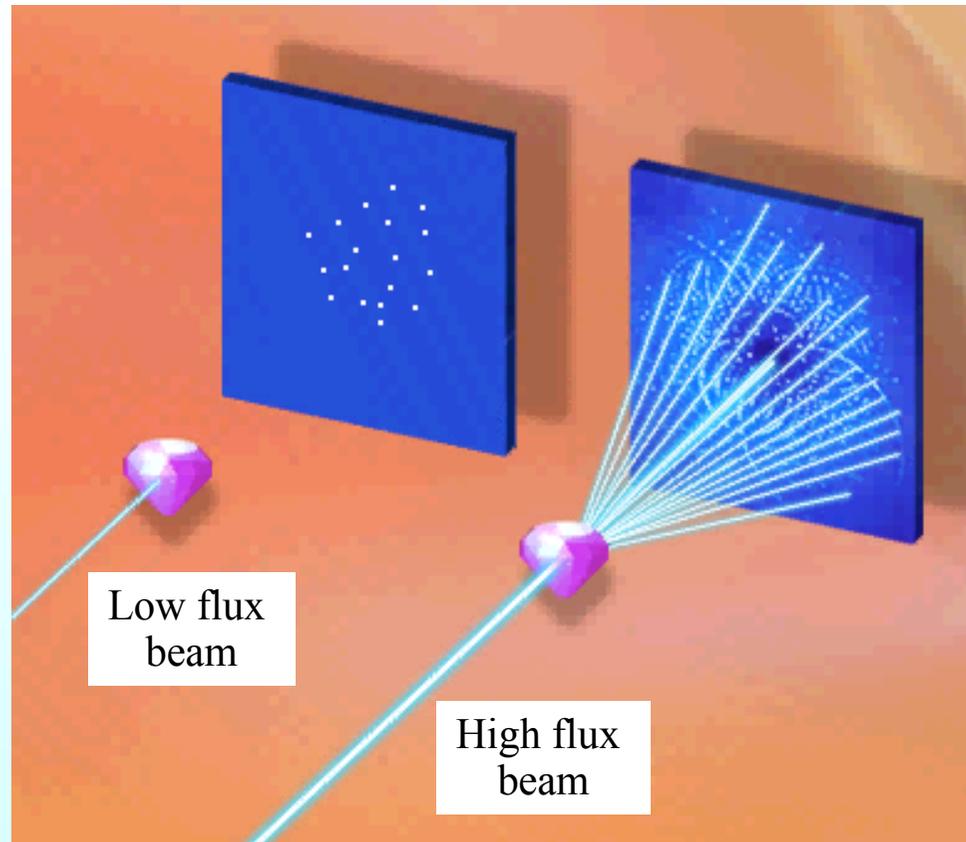
Absorption



Imaging



Laue Diffraction

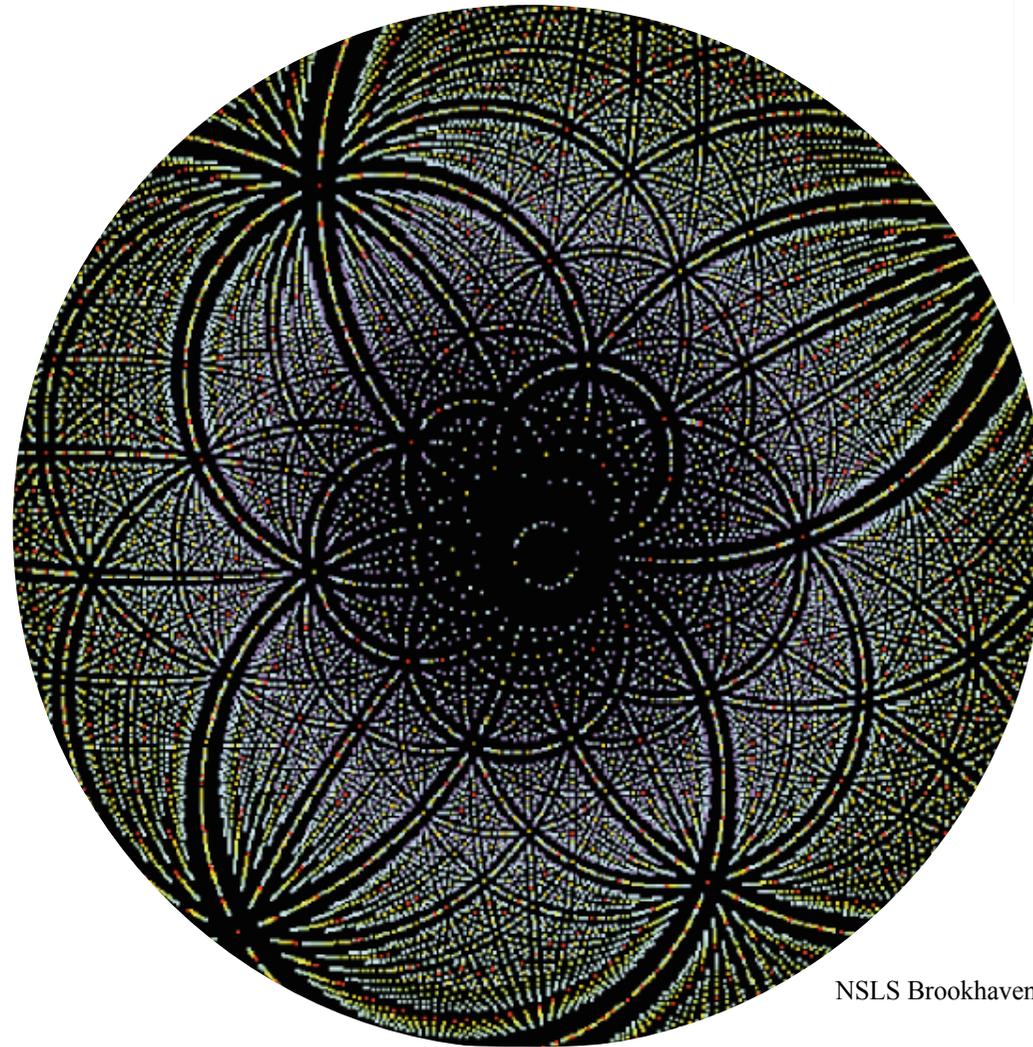


Synchrotron light, Springer-Verlag Compact Disk 2000



Giuseppe Dalba, University of Trento, Italy

Laue pattern of a crystal of metabolic enzyme isocitrate dehydrogenase



NLS Brookhaven

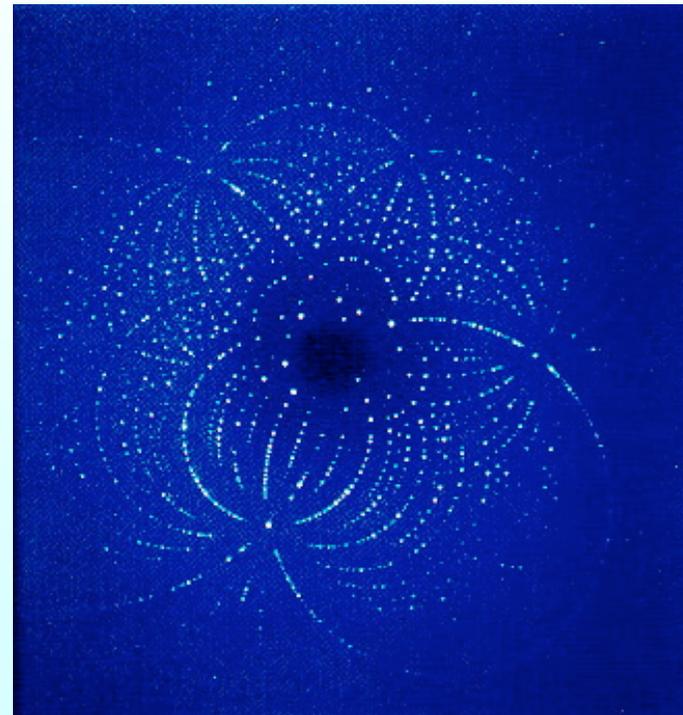
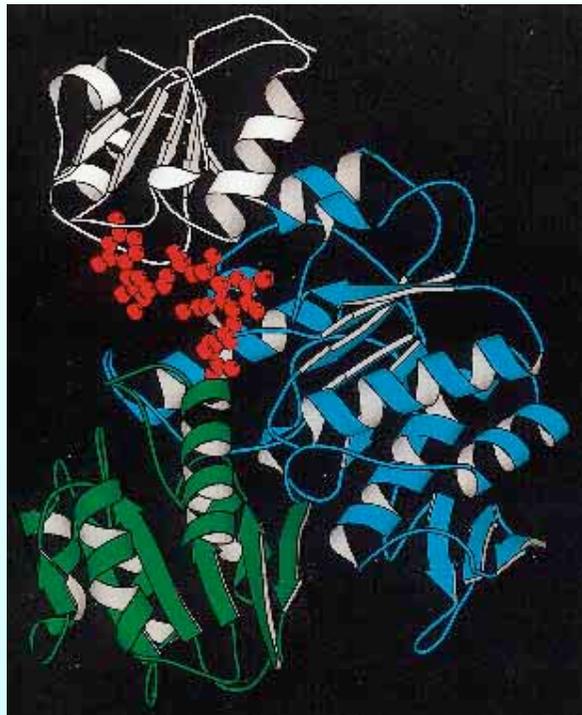
Time resolved crystallography: Exposure time: 10 ms



Giuseppe Dalba, University of Trento, Italy

Biology

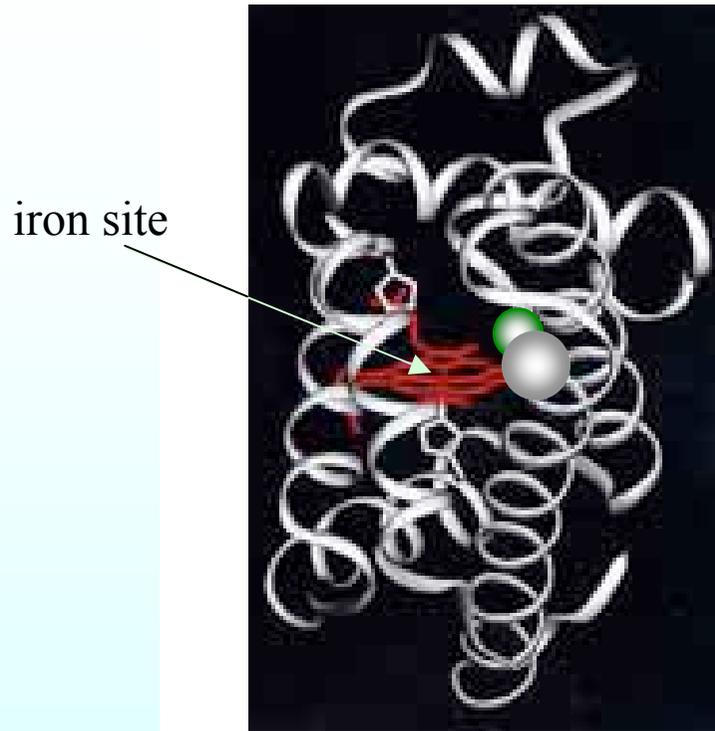
The functions of the life molecules, like proteins and nucleic acids, depend on three-dimensional atomic structure. For instance the knowledge of viruses has allowed the preparation of anti-viruses compounds to be prepared



Diffraction is the technique to study the molecular structure of biological systems



Film of molecular process



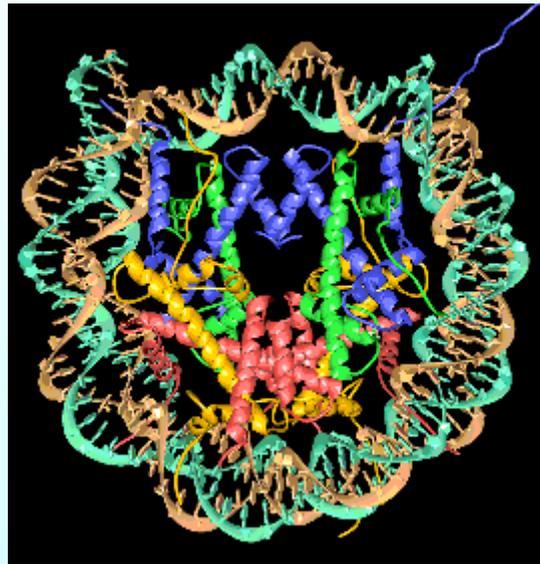
The myoglobin molecule

a CO molecule interacting with a myoglobin molecule



The life construction plan reported by the genetic code

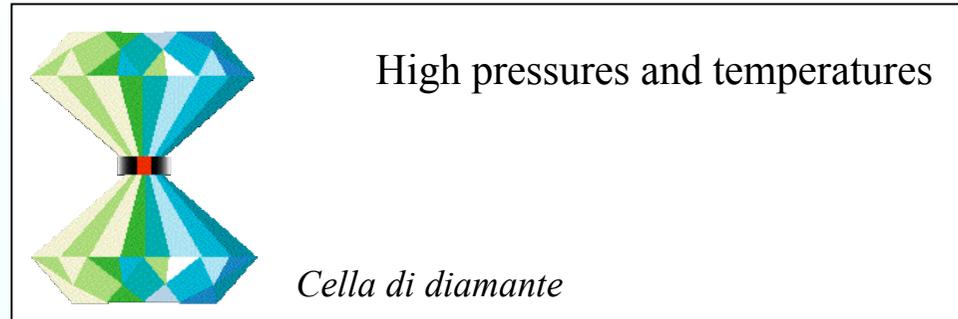
The collection of precise information on the molecular structure of chromosomes and their components can improve the knowledge of how the genetic code of DNA is maintained and reproduced



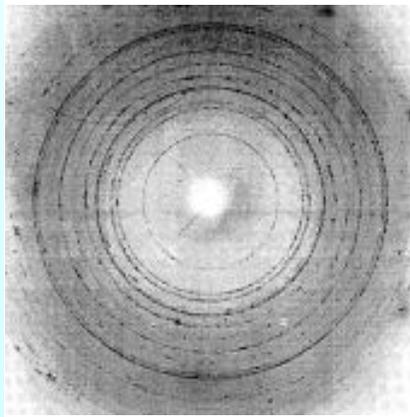
Reconstruction of the molecular structure of nucleosome with a resolution of .2 nm



Study o materials under extreme conditions



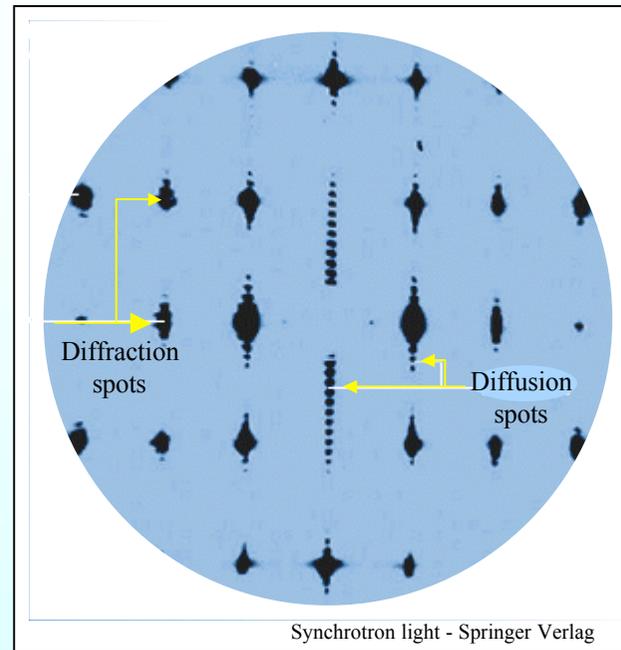
In laboratory it is possible to reach pressures of some millions of atm (100 Gpa) comparable with those present in the Earth nucleus



Iron is the dominant element present in the nucleus of the Earth. The knowledge of iron properties at high temperature and pressure is fundamental for Earth science. At ESRF a new orthorombic phase of Fe has been discovered at 45 GPa and 2100 K



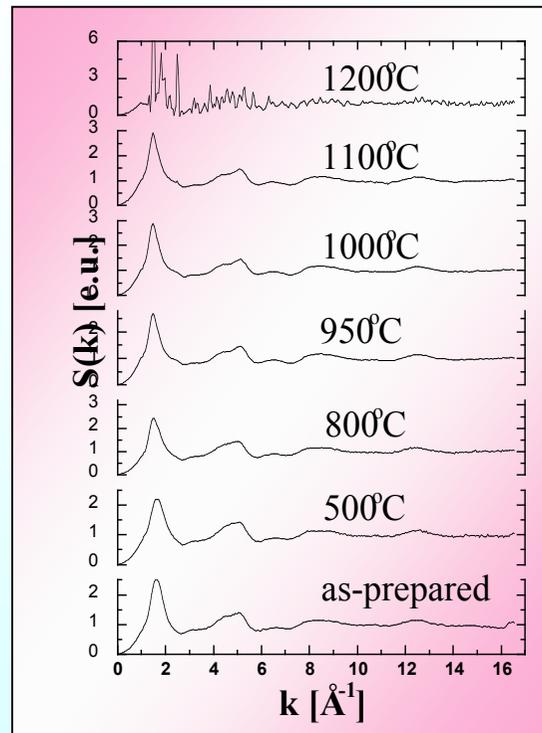
Diffuse scattering in crystalline materials



Unexpected diffusion peaks appear in a diffraction pattern of a non perfect crystalline structures.



Diffuse scattering in amorphous materials

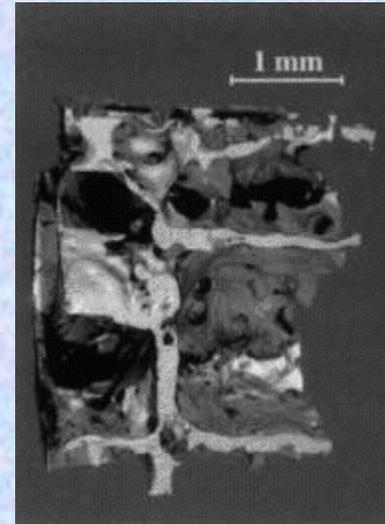
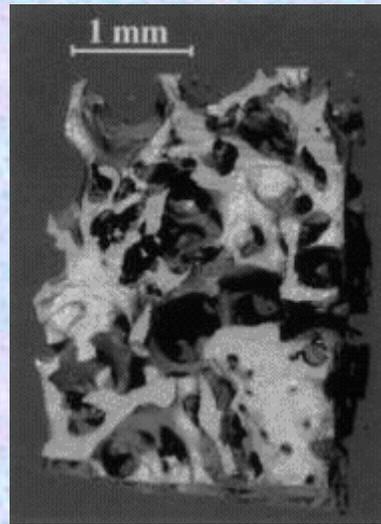
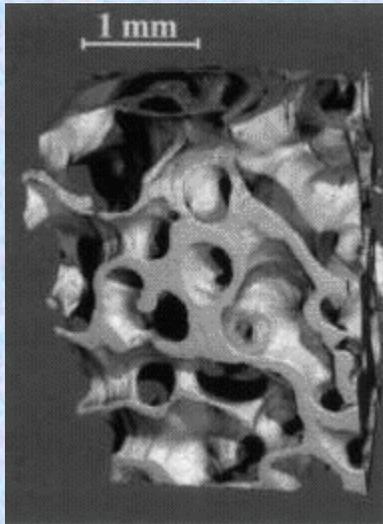


The structure factors for pure silica gel samples treated at different temperatures starting from the as-prepared to 1200°C.

WAXS measurements can be carried out in short time at various conditions of temperature and pressure.



X-ray ray micro-tomography



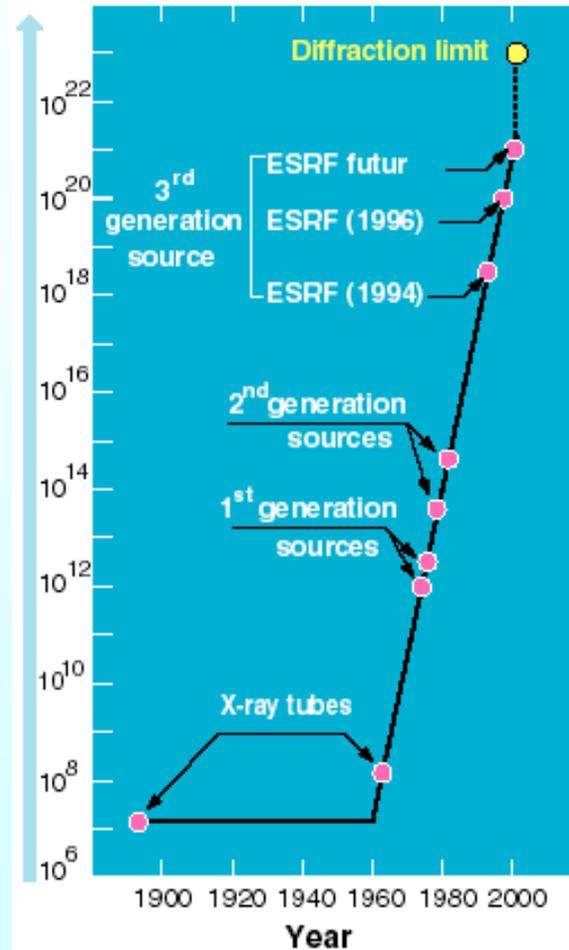
Micro tomogram of iliac crest bone from a female patient undergoing haemodialysis. The three images are of biopsies taken at three ages, 24, 27 and 32 years. The severe loss of bone mass is apparent.

The ratios of bone volume to total volume fell from 29.6% to 23.7% between the ages of 24 and 32

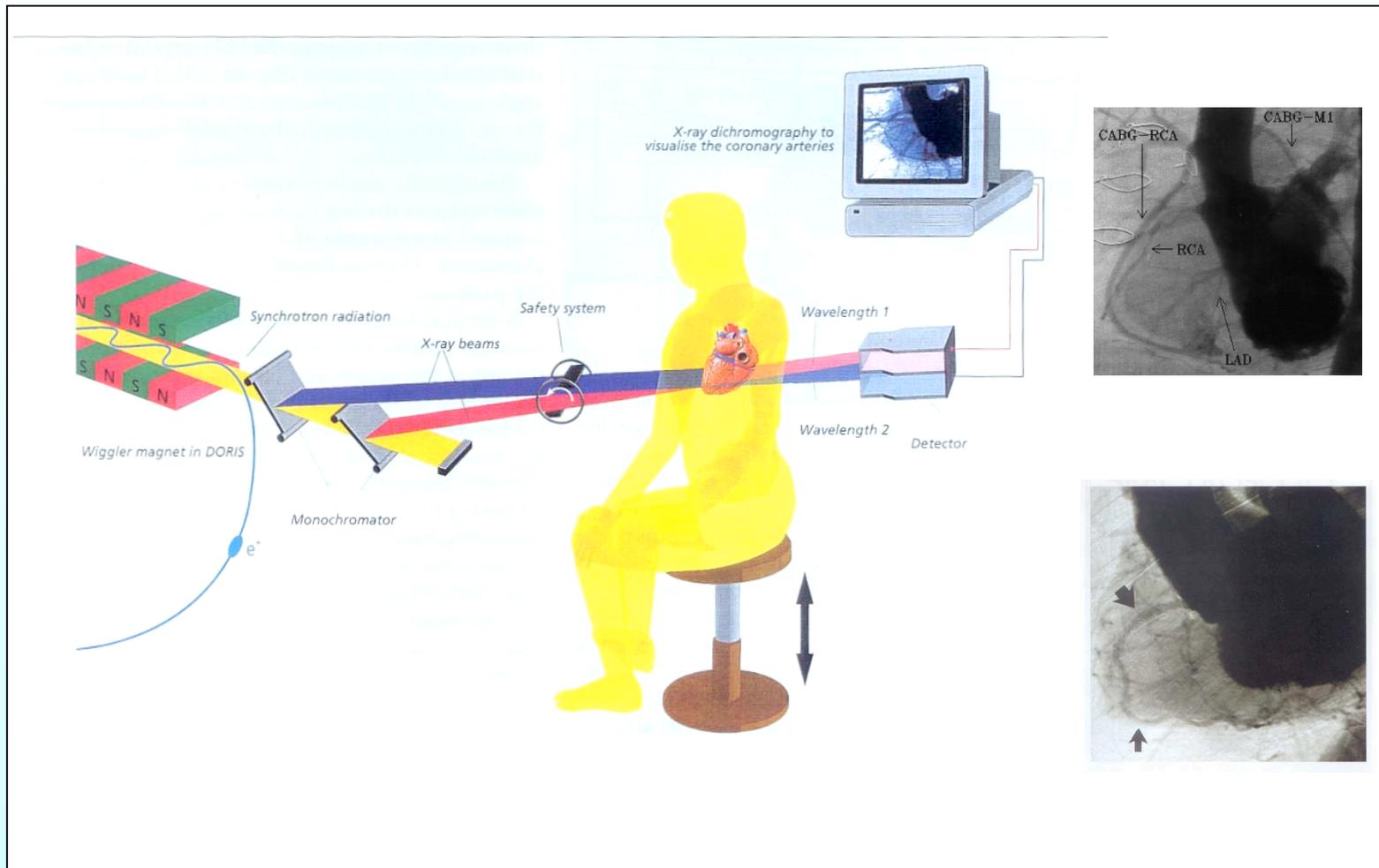


The brilliance versus time

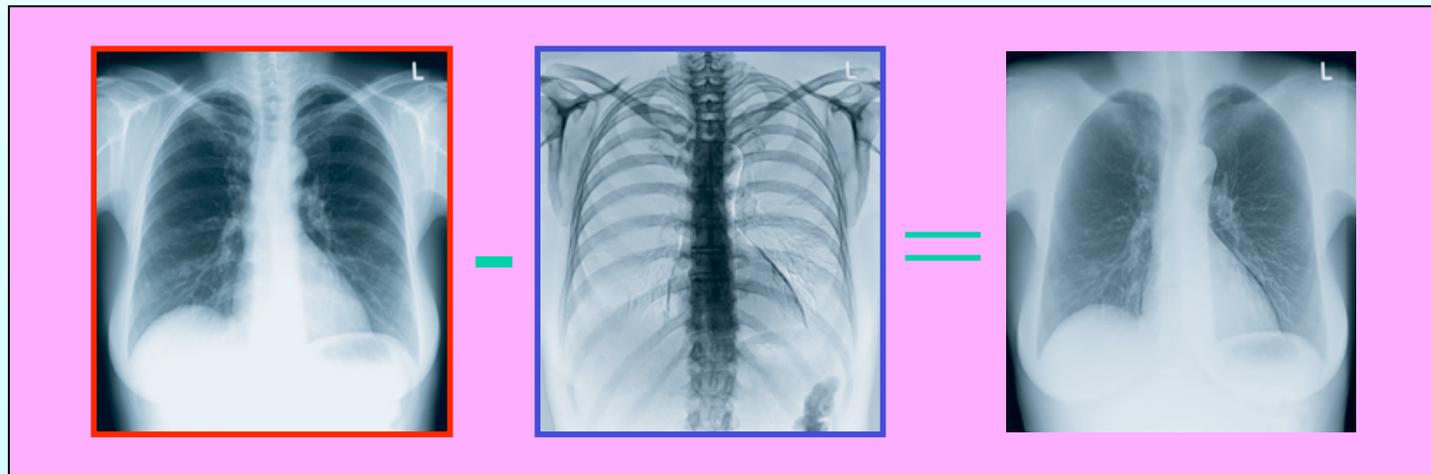
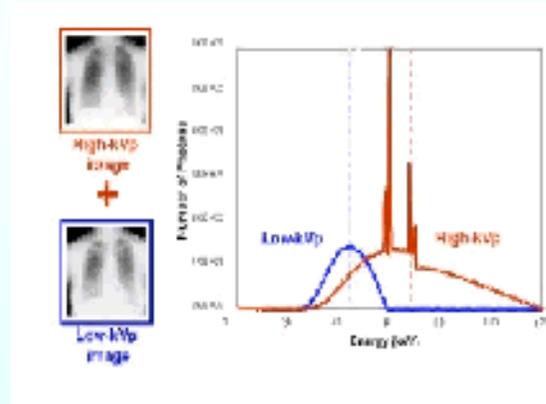
Brilliance of the X-ray beams
(photons / s / mm² / mrad² / 0.1% BW)



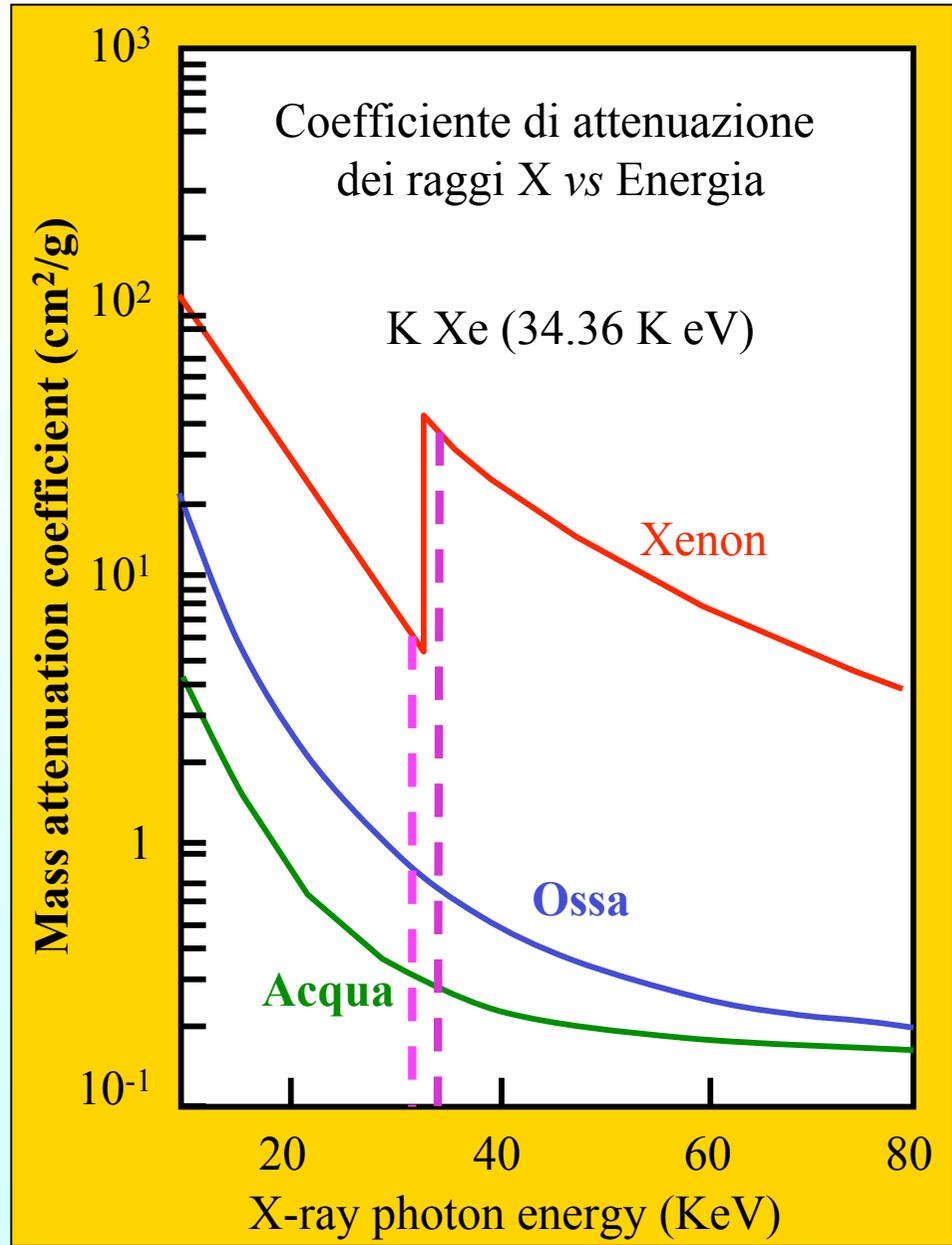
Coronary angiography



Dual Energy Subtraction Radiography



Dual Energy Subtraction with contrast element



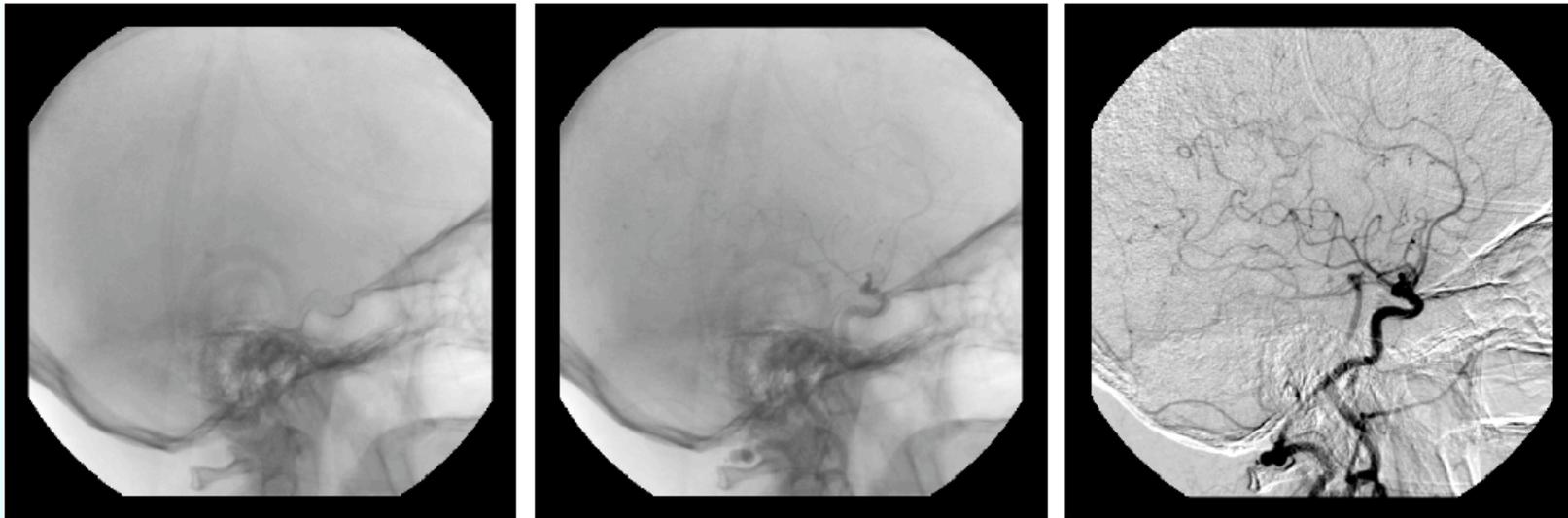
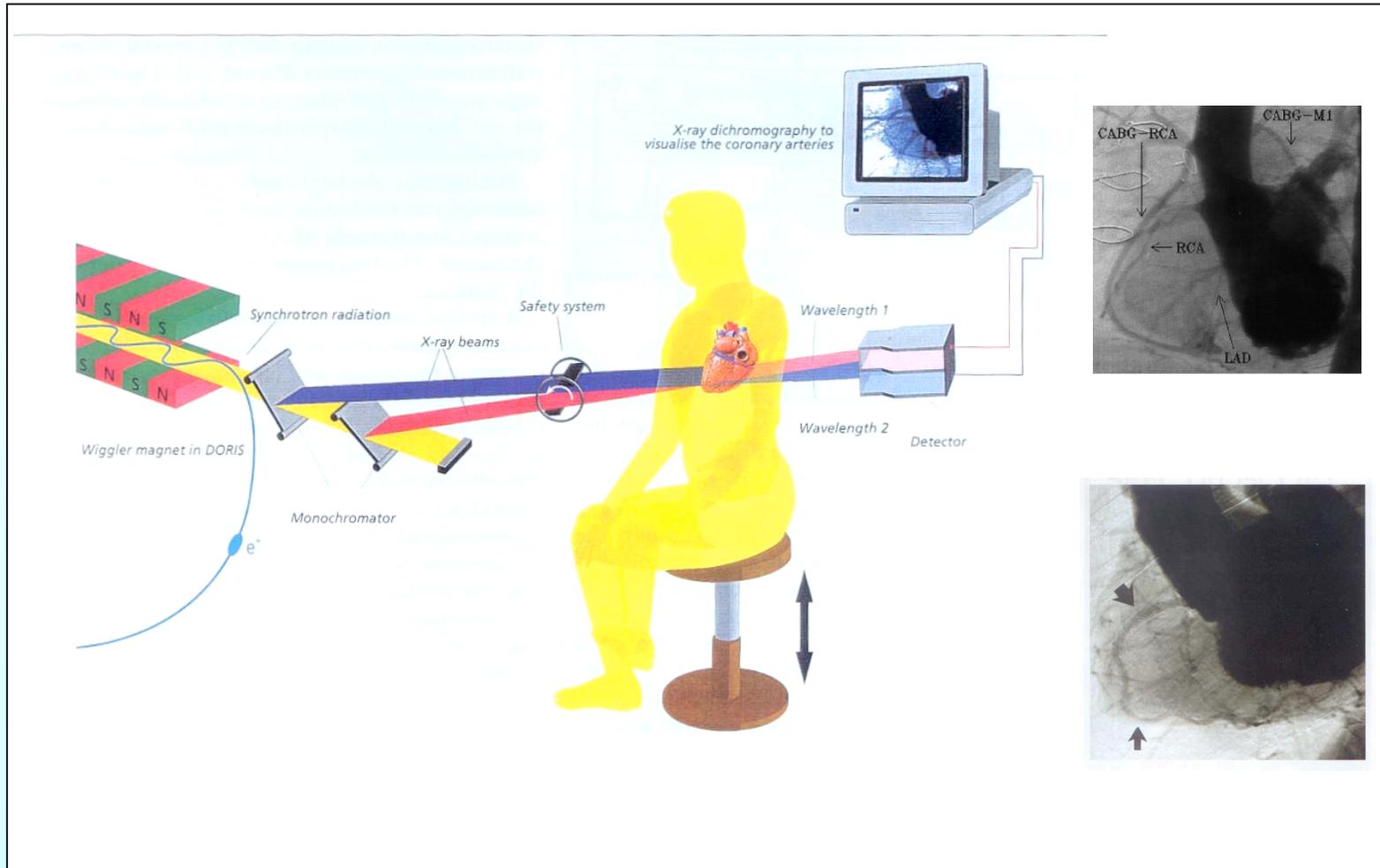


Figure 1: An example of motion artifacts in a cerebral DSA image (right), obtained by subtraction of the mask image (left) from the contrast image (middle), and subsequent image-contrast enhancement. The artifacts appear as black and white structures.



Coronary Angiography



BRONCHOGRAPHY

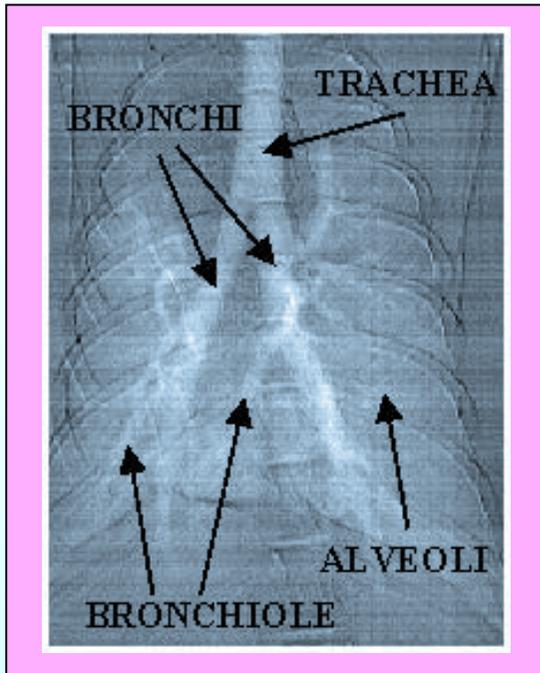
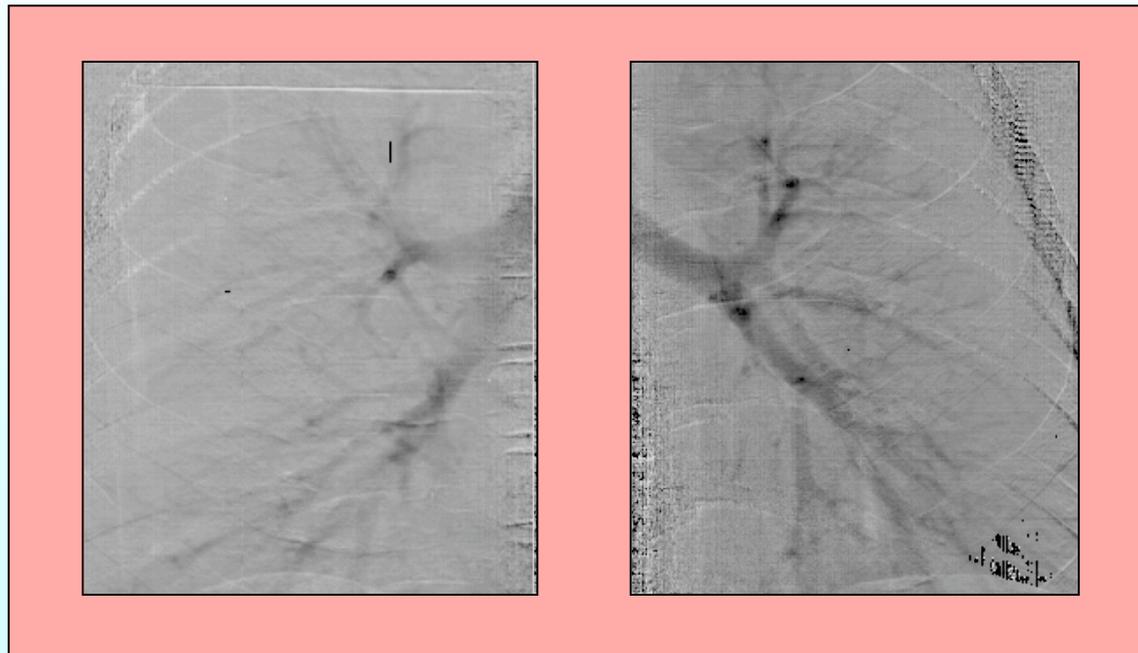


Immagine *in vivo* ottenuta mediante sottrazione digitale dei polmoni di un topo mostrante la distribuzione dell'agente di contrasto, Xenon, nell'albero bronchiale.

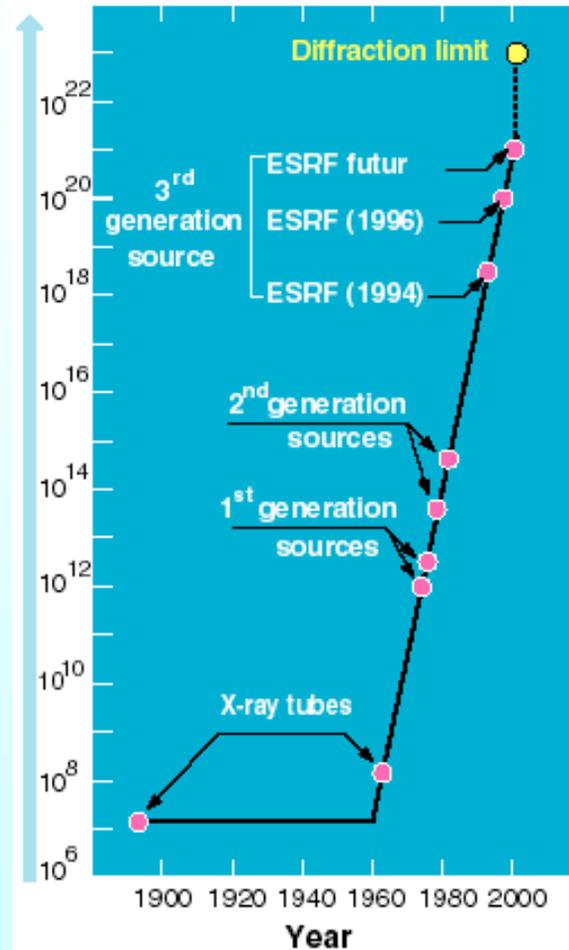
L'obiettivo è di vedere I dettagli morfologici dei bronchi ed il riempimento degli alveoli Durante il ciclo respiratorio in presenza di xenon nelle vie respiratorie.





The brilliance versus time

Brilliance of the X-ray beams
(photons / s / mm² / mrad² / 0.1% BW)



Bibliography

Synchrotron light, Springer-Verlag Compact Disk 2000, ISBN 3540148884.

100 anni di Raggi X, 2001, P. Fornasini, Università degli Studi di Trento
Dipartimento di Fisica, Compact Disk, 2001

<http://www.elettra.trieste.it> (web site of Italian Synchrotron Light Source, named ELETTRA, Trieste Italy))

<http://www.sesame.htm>

<http://www.esrf.fr> (web site of European Synchrotron Radiation Facility, Grenoble, France)

<http://www.lbl.gov/MicroWorlds/ALSTool/> (web site of the Advanced Light Source)

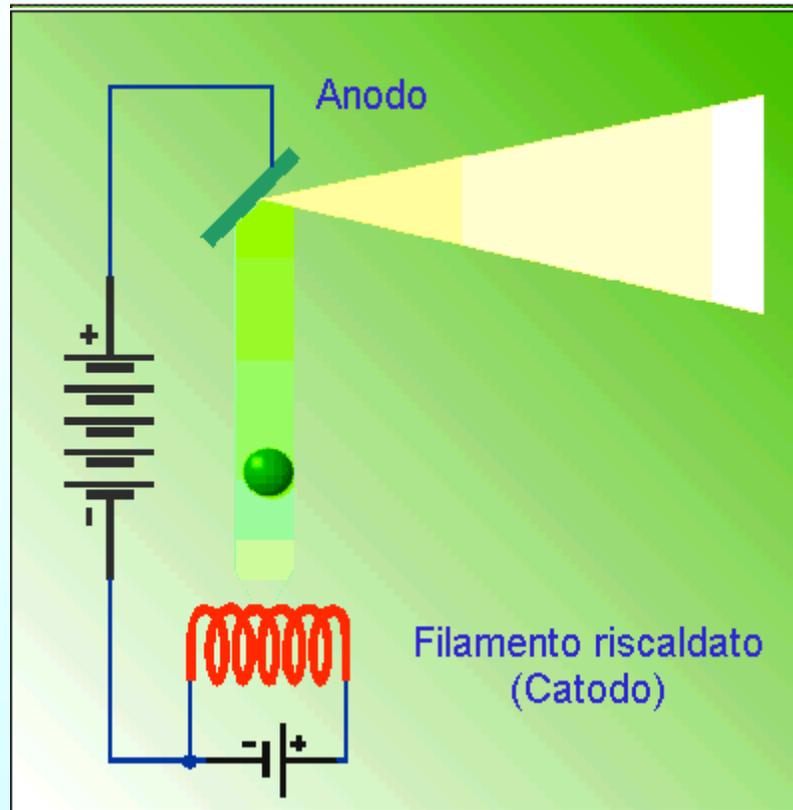
Time Resolved Macromolecular Crystallography, *Physics Today*, 54 (2001) 33.
Mr. Tompkins in paperback by G. Gamow

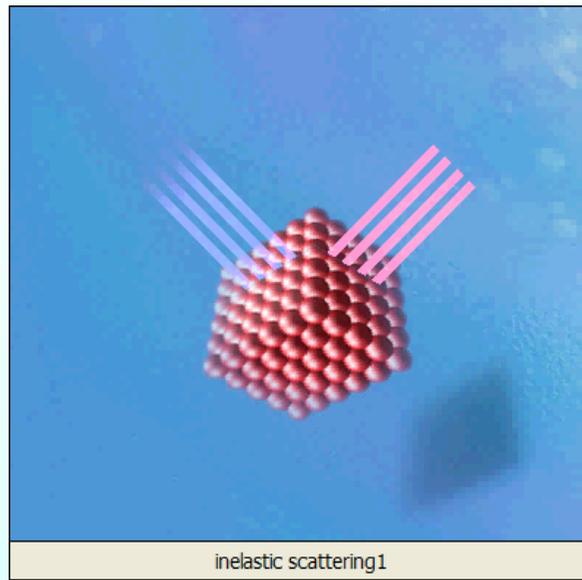
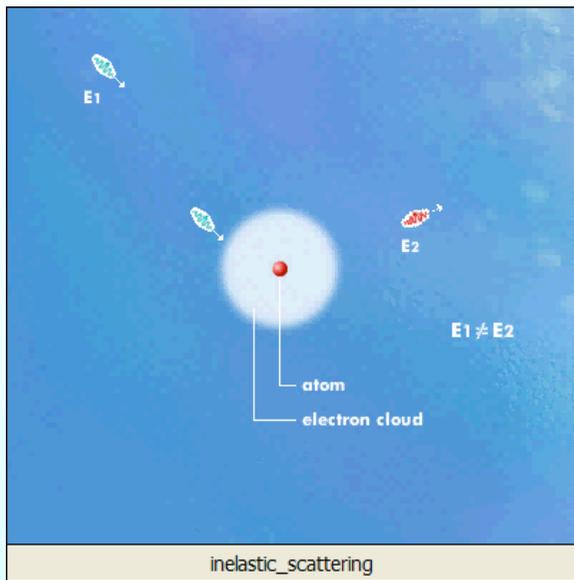
J Als-Nielsen, *Des McMorro* *Elements of modern X-ray Physics* Wiley





Emission from an x-ray tube

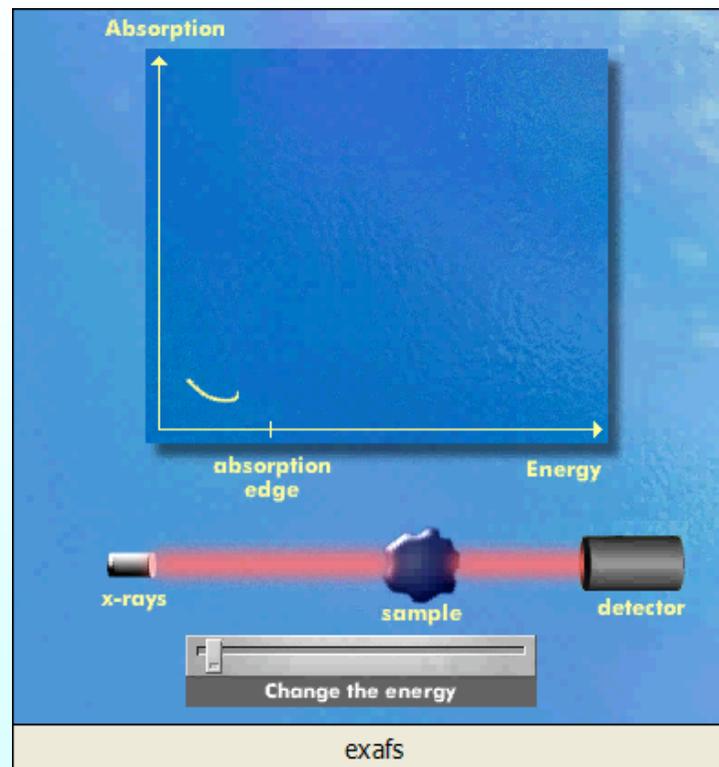




Synchrotron light, Springer-Verlag Compact Disk 2000



Giuseppe Dalba, University of Trento, Italy

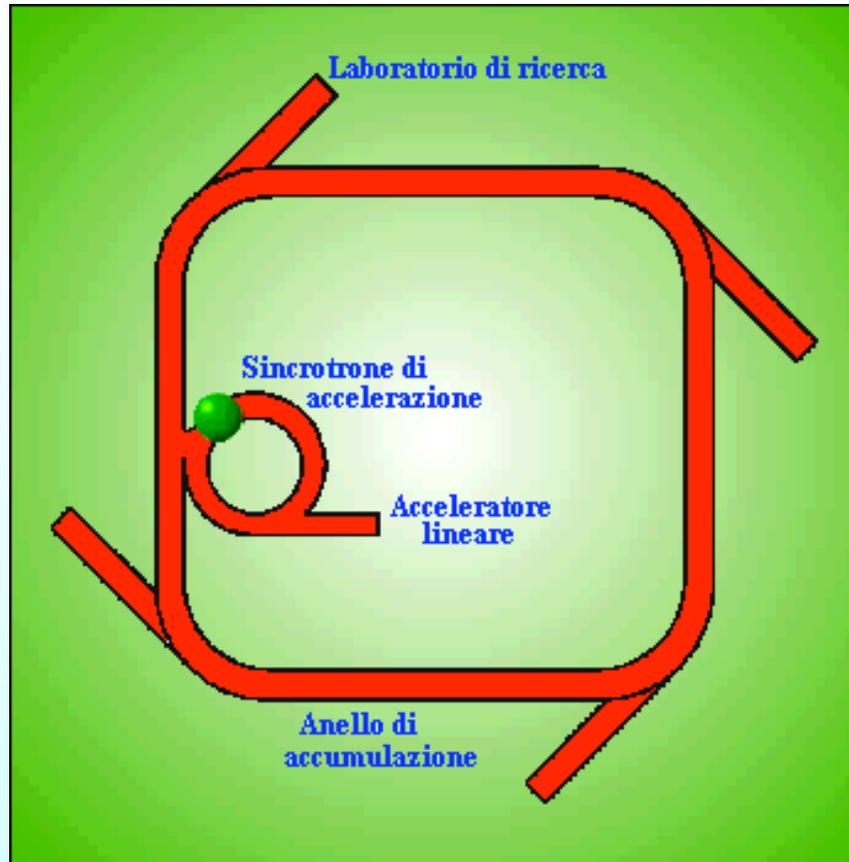


Synchrotron light, Springer-Verlag Compact Disk 2000



Giuseppe Dalba, University of Trento, Italy

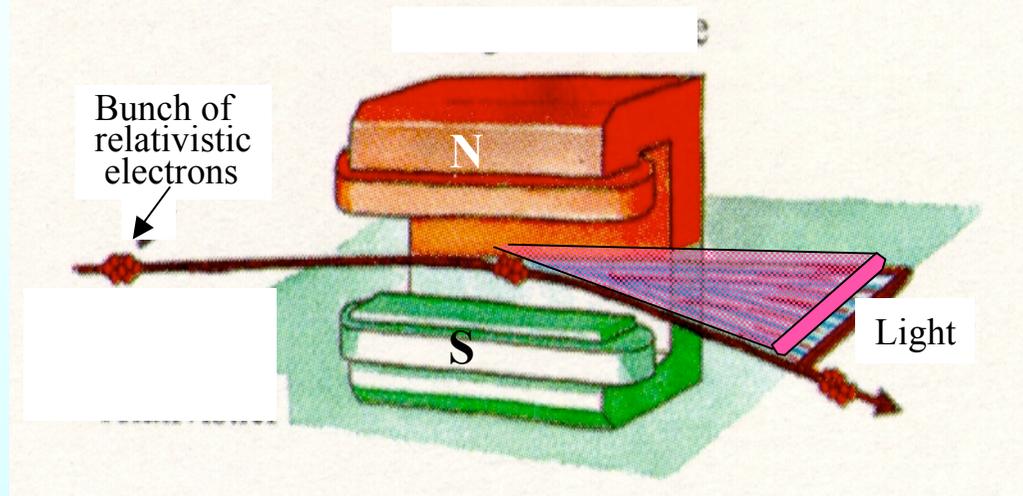
Charged particles in accelerated motion radiate



Storage ring



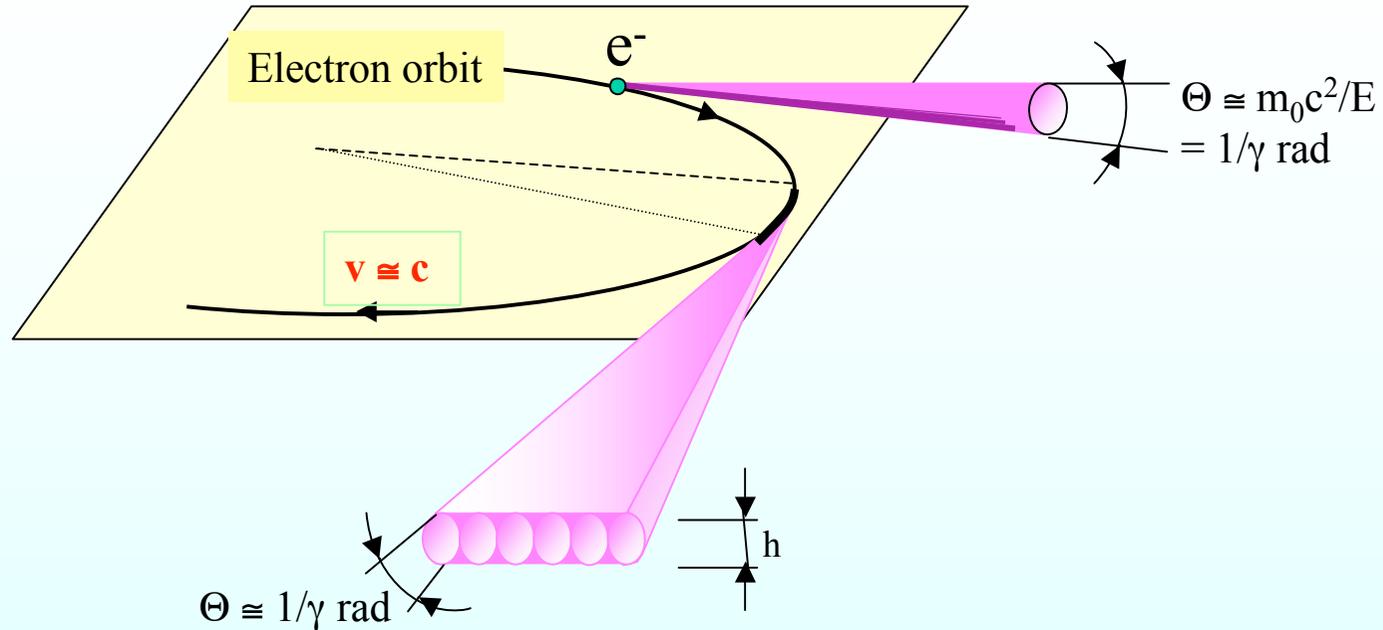
Bending magnet



Storage ring



Angular divergence



The beam collimation is defined as the photon opening angle $\Theta \approx 1/\gamma$ rad. For GeV electrons Θ can be smaller than 0.1 m rad. It means that at 100 m from the source the vertical dimension of the beam, h , is 1 cm.

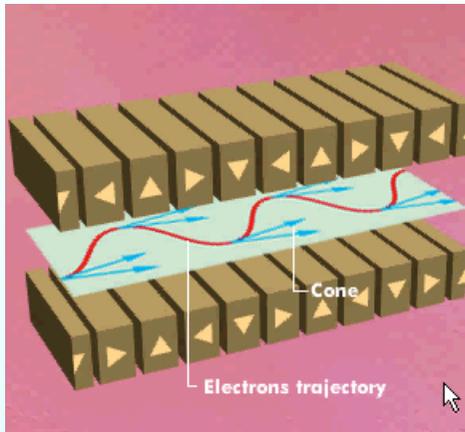
Horizontally the beam opens as a fan. A very thin sheet of light spreads out from the orbit on the orbital plane.



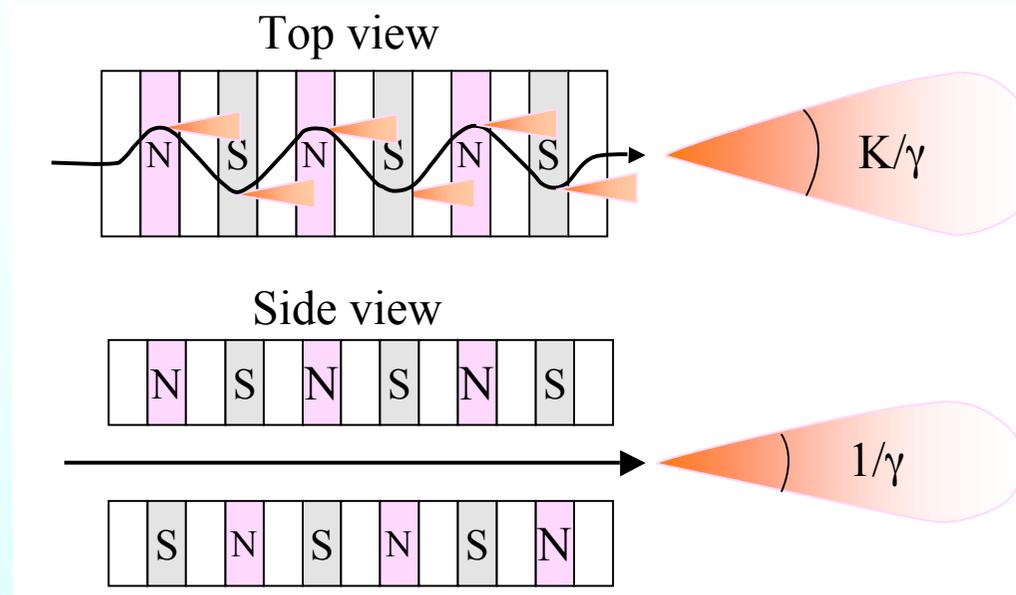
Properties



Wiggler



Synchrotron light, Springer-Verlag Compact Disk 2000



Radiation from a wiggler: the horizontal opening is higher than the vertical one: K is around 20 for a wiggler



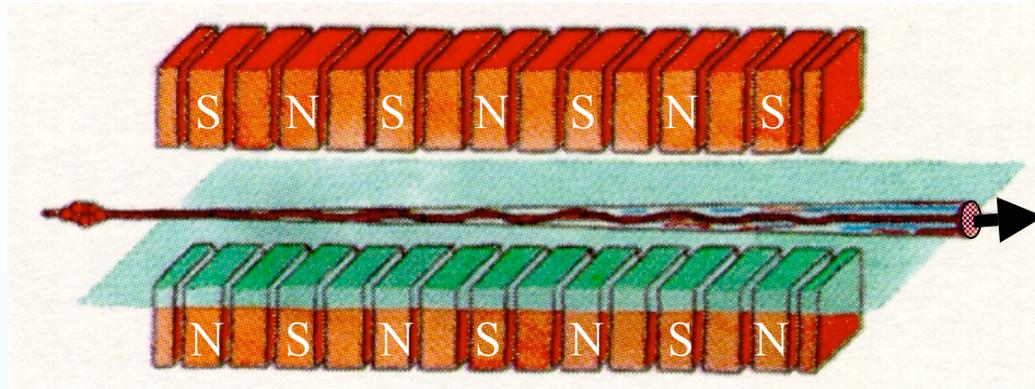
Storage ring



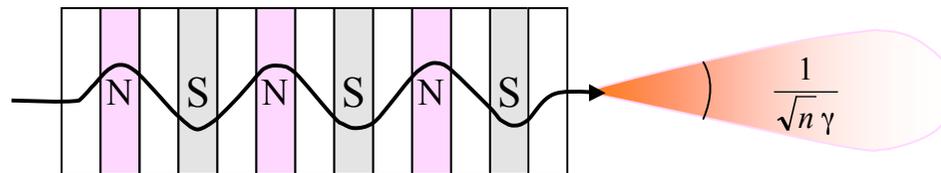
Properties



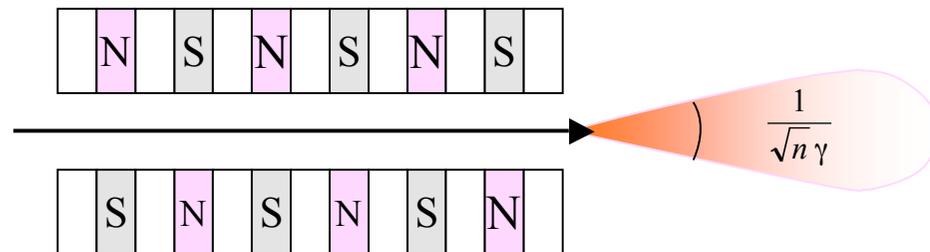
Undulator



Top view



Side view



Collimation, Why?



Storage ring

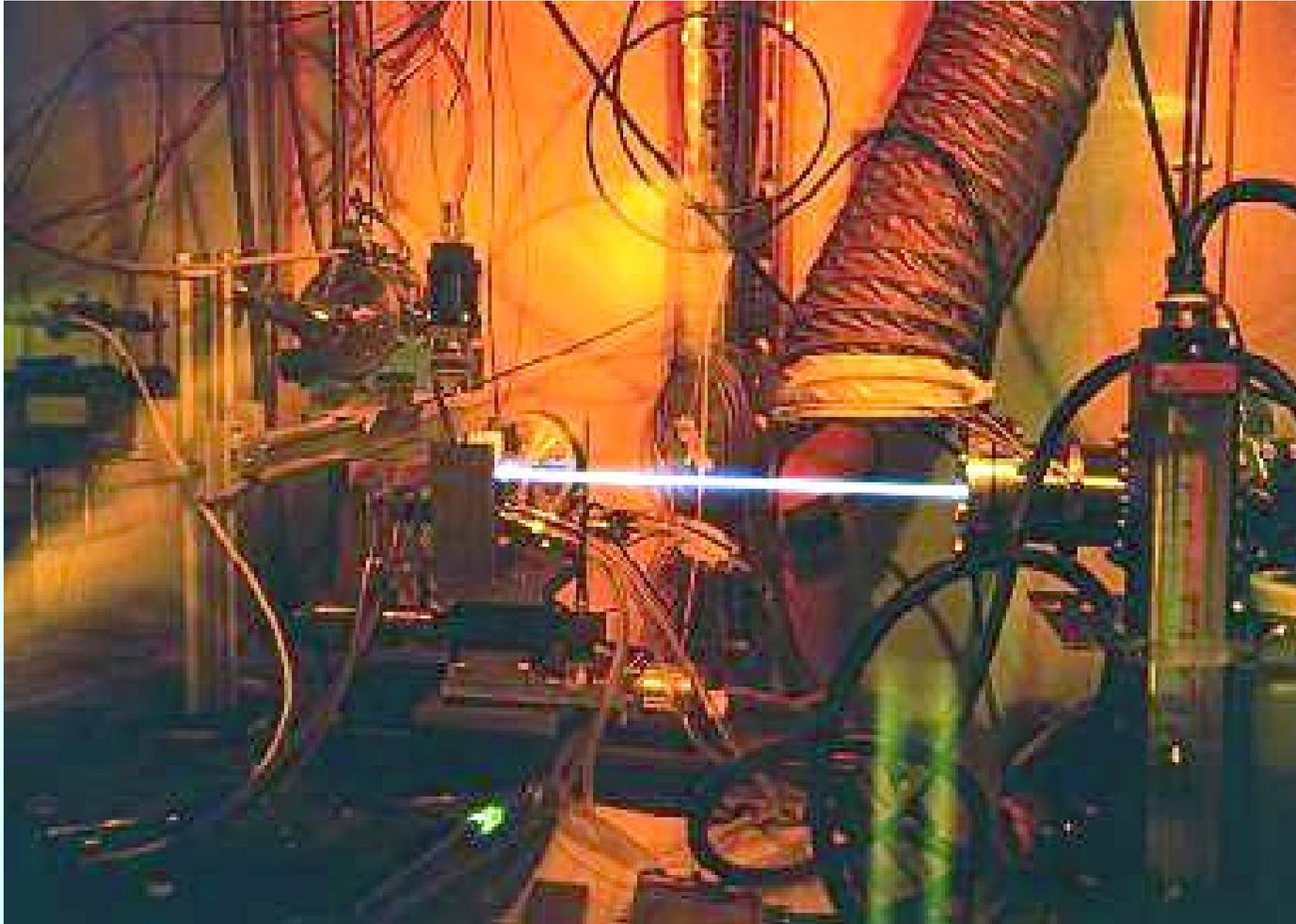


Properties

Radiation from an undulator: typically $N = 50$



An X-ray beam at the ESRF facility



Are X-rays visible?

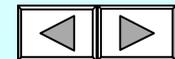
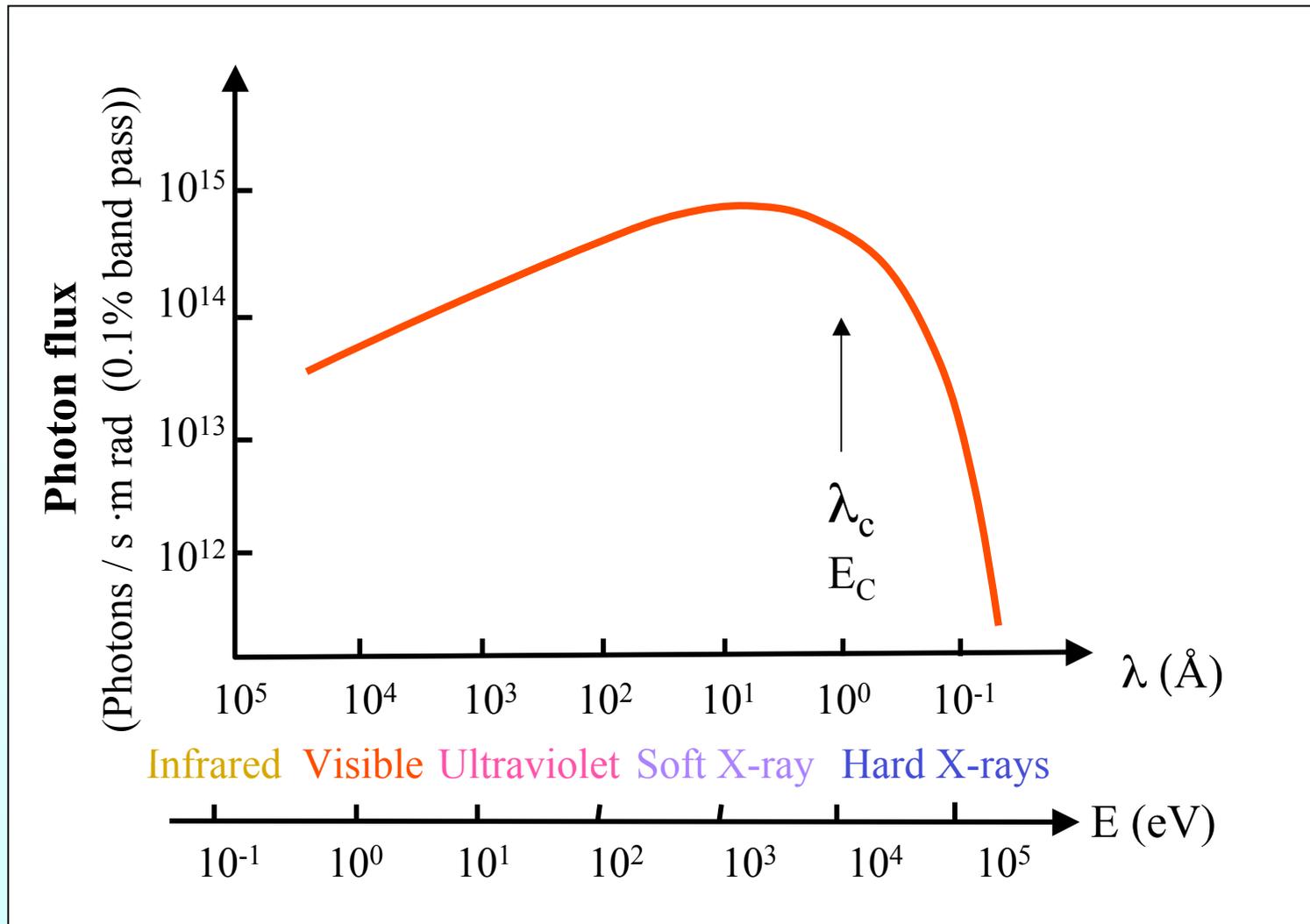


Properties

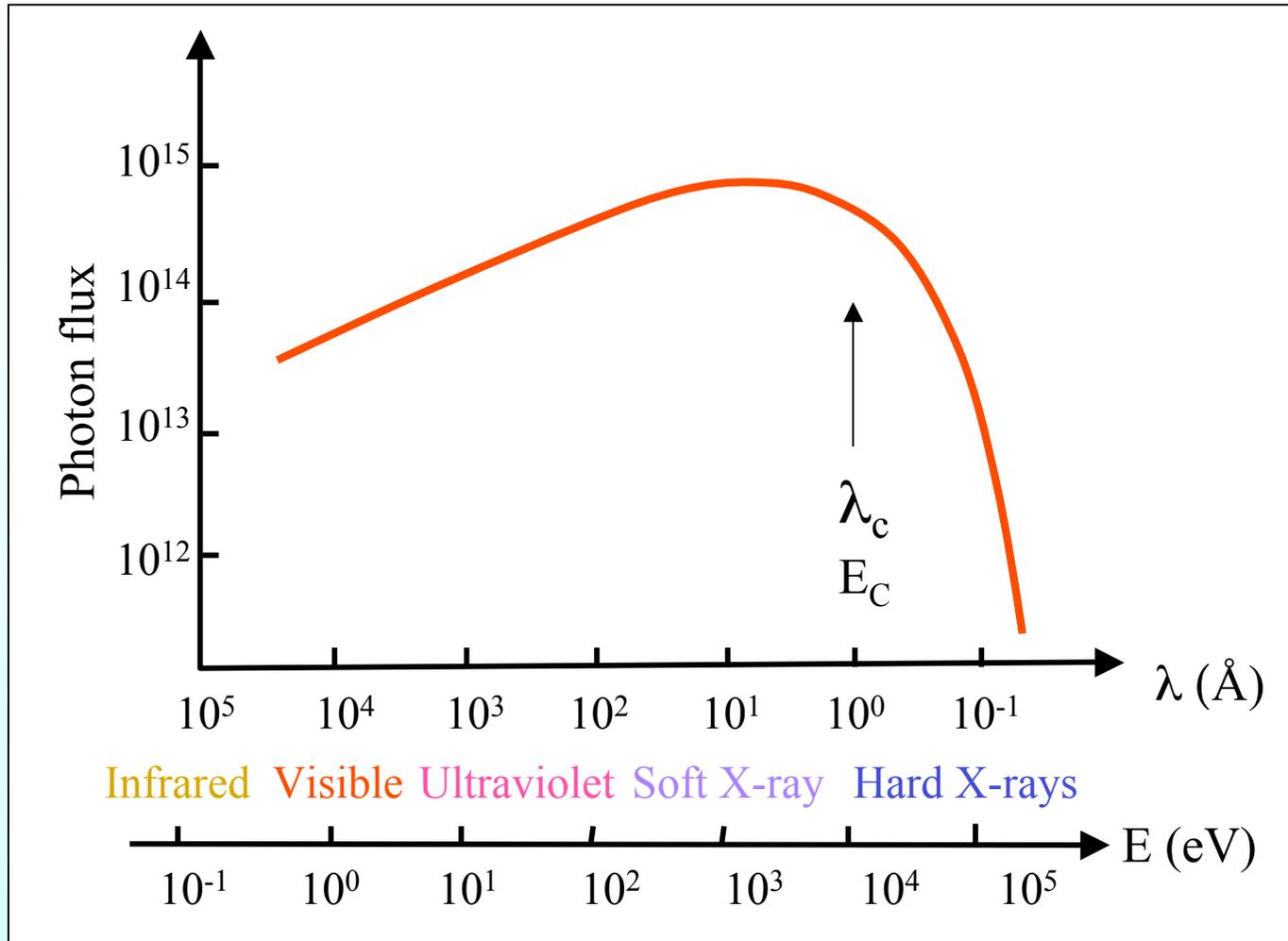


Giuseppe Dalba, University of Trento, Italy

Flux of synchrotron light .



Spectral distribution of synchrotron light .



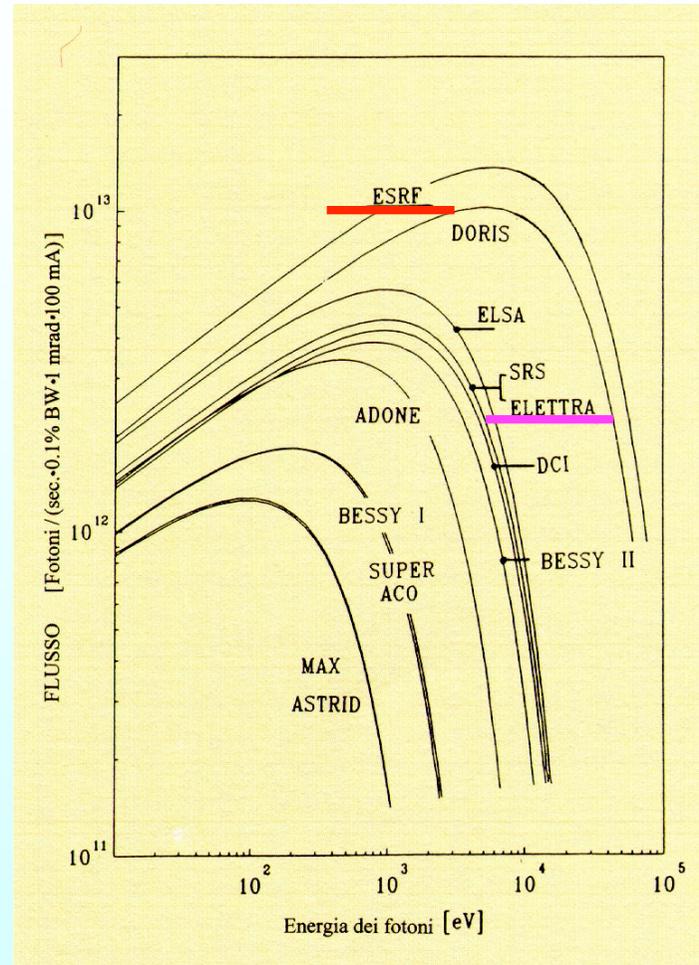
$$\lambda_c = \frac{5.6 R}{E^3} = \frac{18.6}{B \cdot E^2}$$



Spectra



Spectral distribution curves from bending magnets of some synchrotron light facilities



Properties

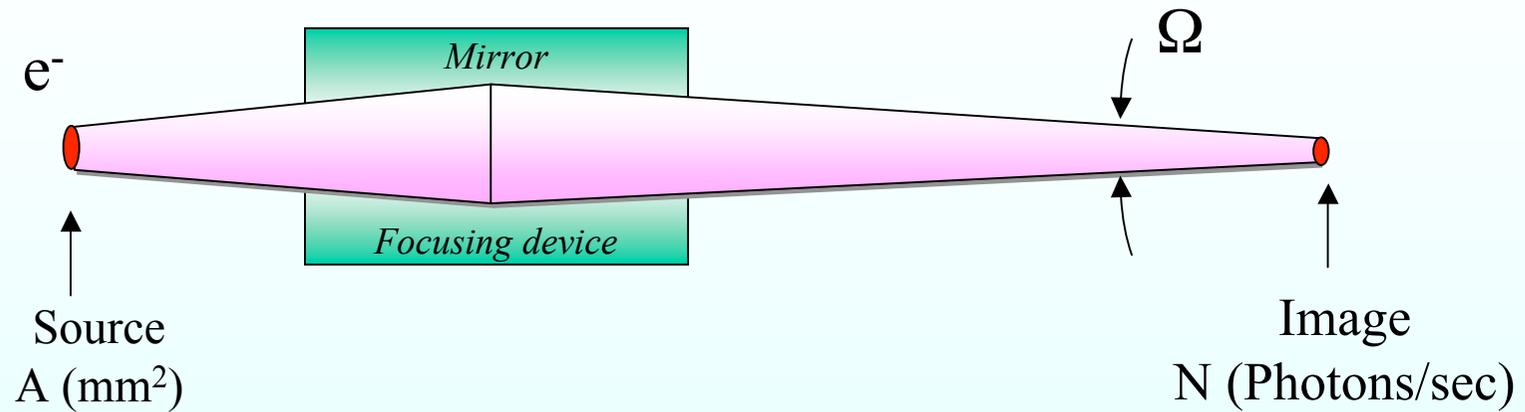


Critical energy

ESRF is the European facility located in Grenoble, ELETTRA, the Italian facility is located in Trieste.



Definition of Brilliance



$$\text{Brilliance} = \frac{N}{A \cdot \Omega} \left(\frac{\text{Photons / sec}}{\text{mm}^2 \cdot (\text{m rad})^2 (0.1\% \text{ ban})} \right)$$

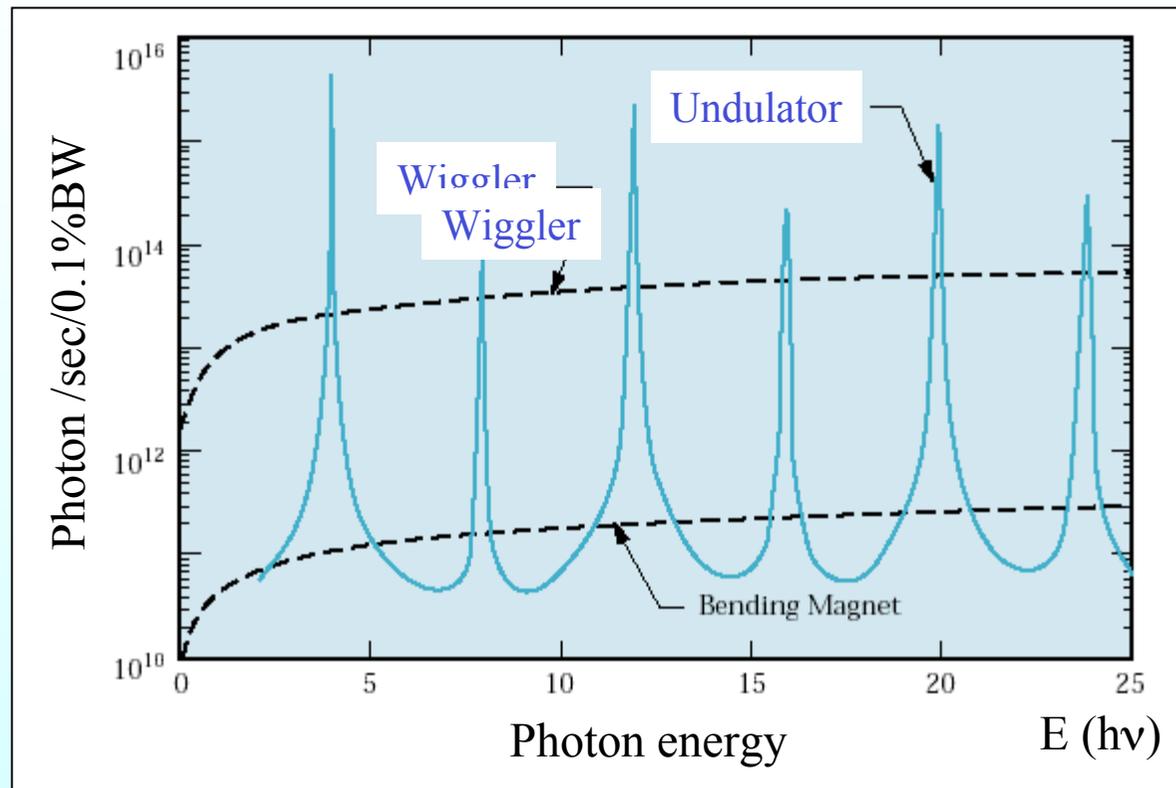
The brilliance represents the largest number of photons per second in a given band pass that can be focused by a perfect optics onto the unit area at the sample



Spectra



Spectral radiation distribution

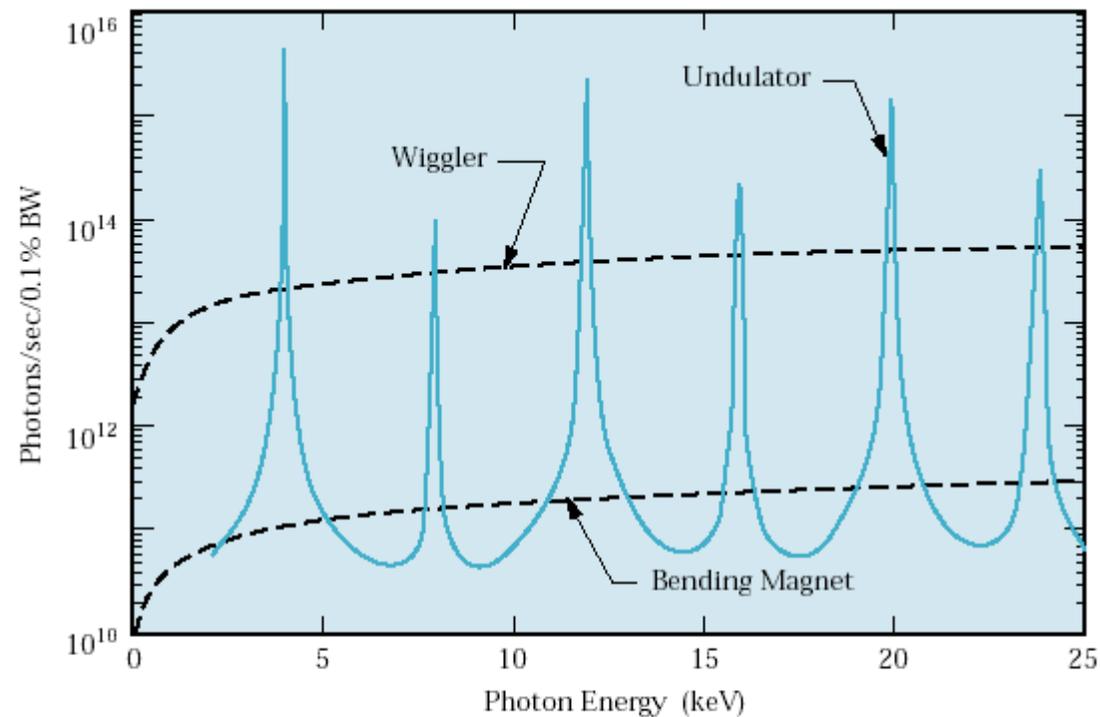


Properties



UHXS Stanford (US)

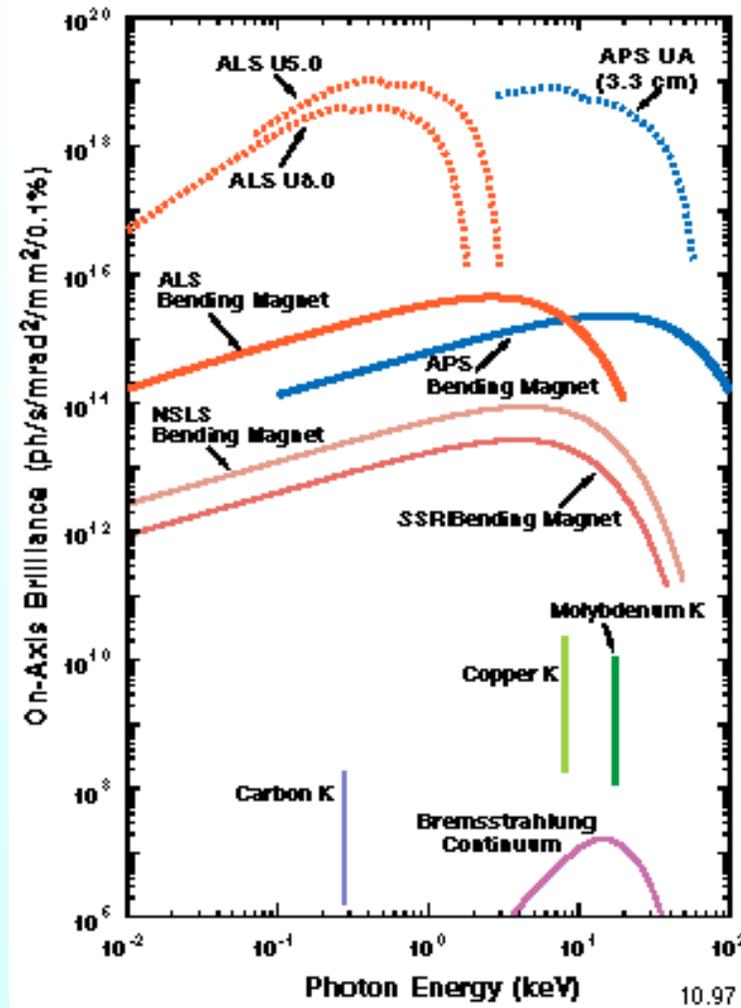




Comparison of spectra produced by an undulator, a wiggler, and a bending magnet type of source installed on the UHXS. The collection aperture is located at a distance of 50 m from the source. The flux is collected over an aperture of $0.5 \times 0.5 \text{ mm}^2$. The bending magnet and wiggler type sources present continuous spectra while the undulator presents a series of intense peaks. The peaks are harmonically related starting from the fundamental around 4 keV. The photon energy of each peak can be tuned by changing the undulator field. The collection of high flux through such a narrow aperture reduces the power to a few hundred watts.



Brilliance

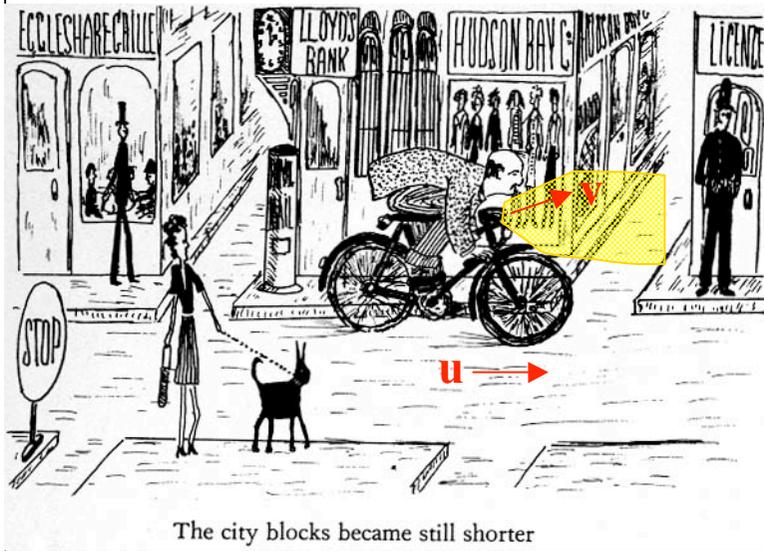


Properties

Comparison of brilliances between synchrotron and conventional x-ray sources

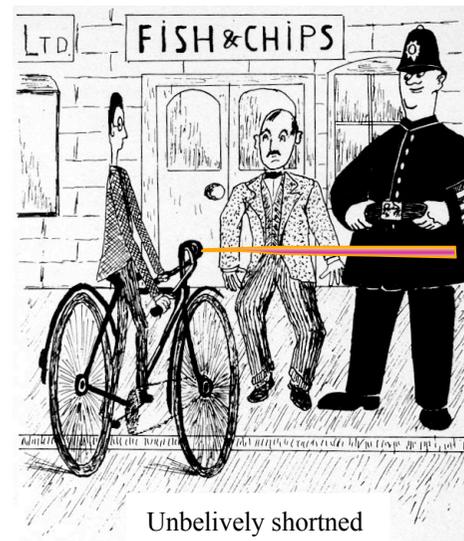


The world as seen from the moving reference frame...



Moving observer

...and from the laboratory reference frame



Lab observer

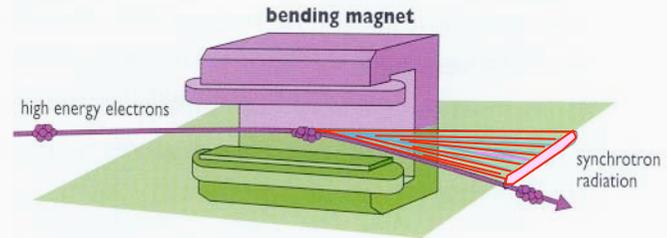
The relativistic effect on the vertical opening of the light beam

Properties

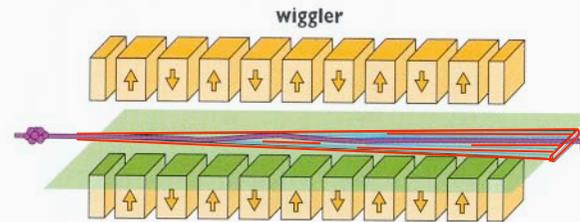


Insertion devices

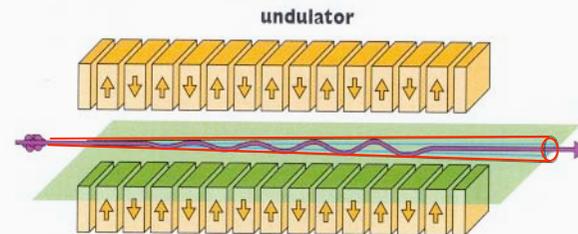
Bending magnets



Wigglers



Undulators



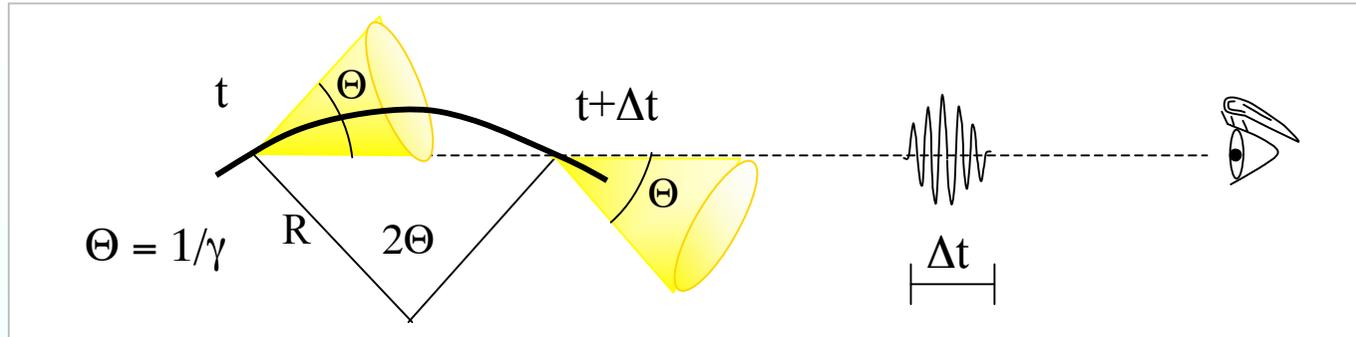
Electron bunches, their trajectory and synchrotron radiation in three different magnetic devices: bending magnets, wigglers, undulators

◀ Storage ring

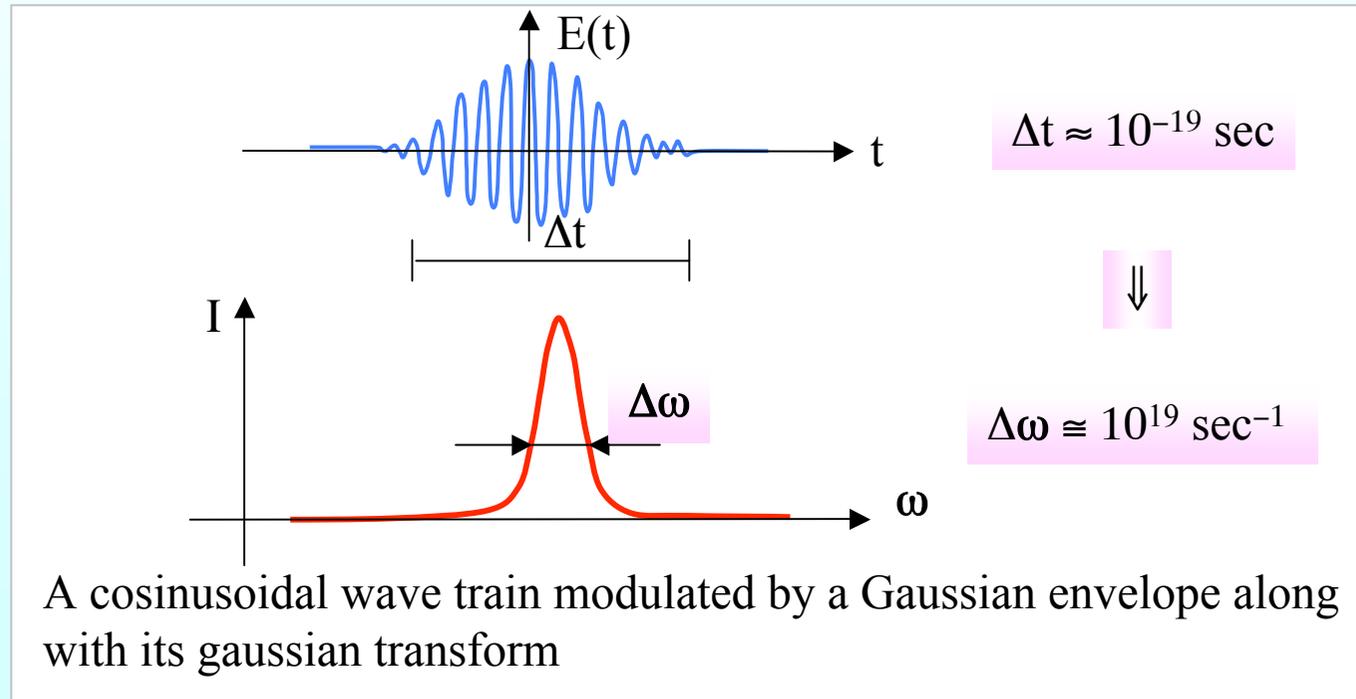


Giuseppe Dalba, University of Trento, Italy

Why a so wide emission spectrum?

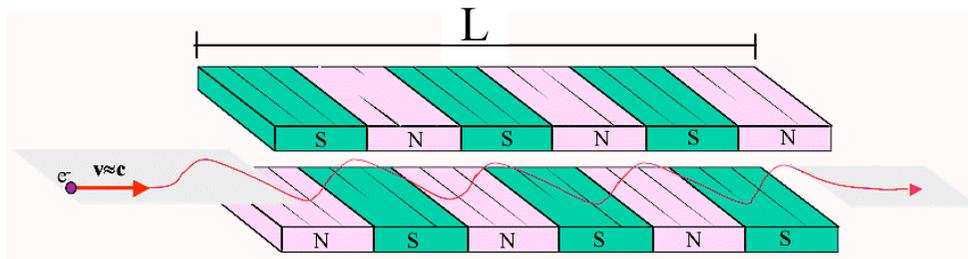


Fourier relationship: $\Delta t \cdot \Delta\omega \approx 2\pi$



Low
wavelengths



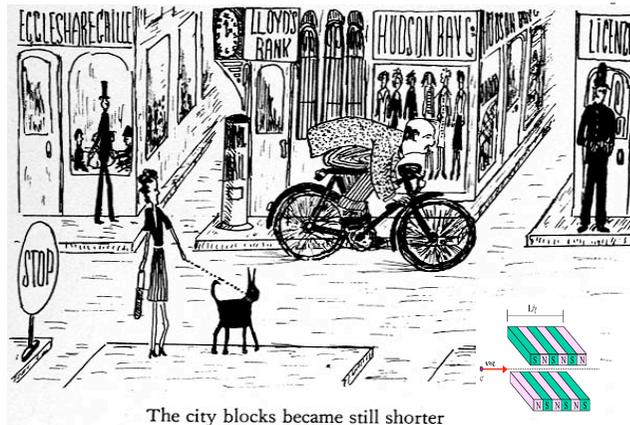


An undulator as seen in the laboratory reference system

$$\lambda_0 = L/n$$

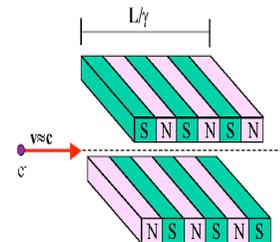
Magnetic pole periodicity

n = number of periods



The city blocks became still shorter

Relativistic contraction

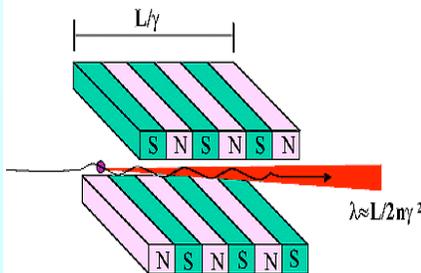


$$\lambda'_0 = L/n\gamma = \lambda_0/\gamma$$

The undulator as seen from the electron

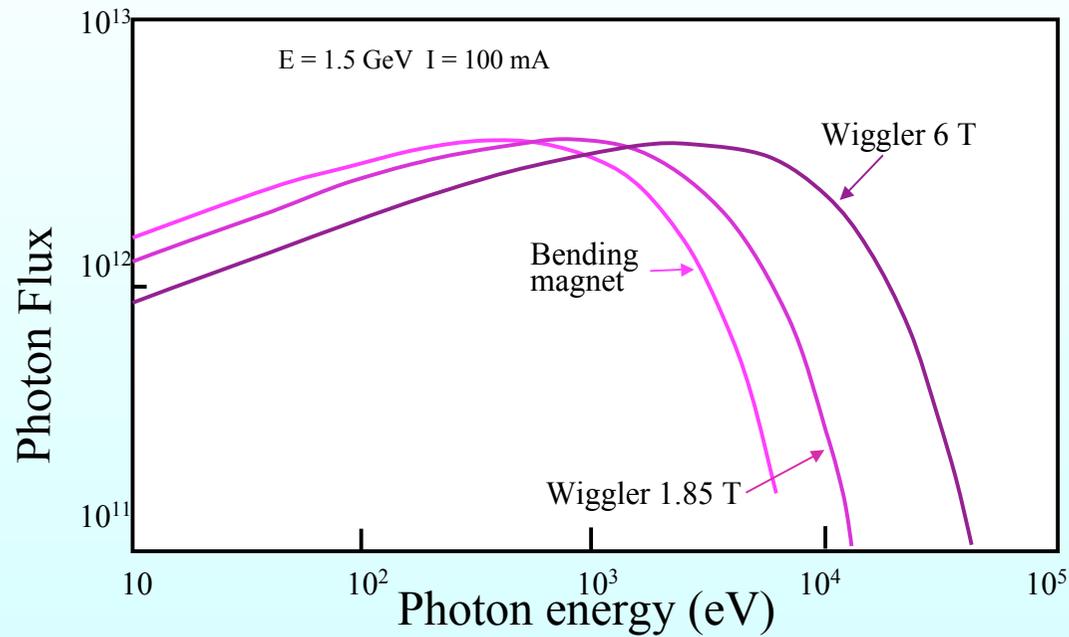
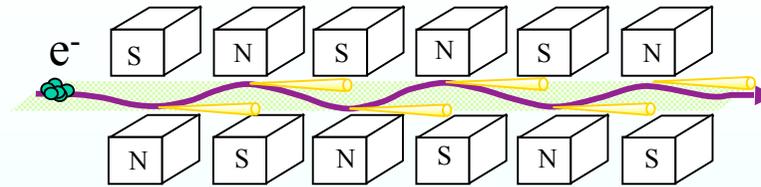
Doppler shift

$$\lambda = L/2n\gamma^2$$



Further reduction of the light periodicity due to the Doppler effect





$$R = \frac{E (\text{GeV})}{B (\text{T})}$$

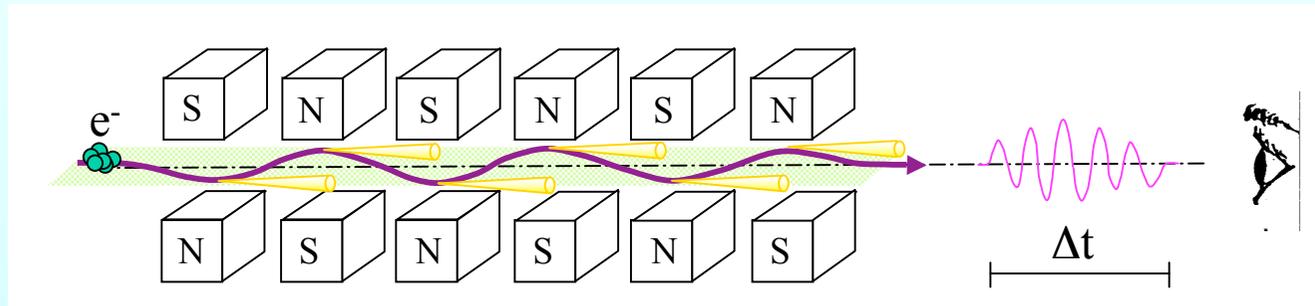
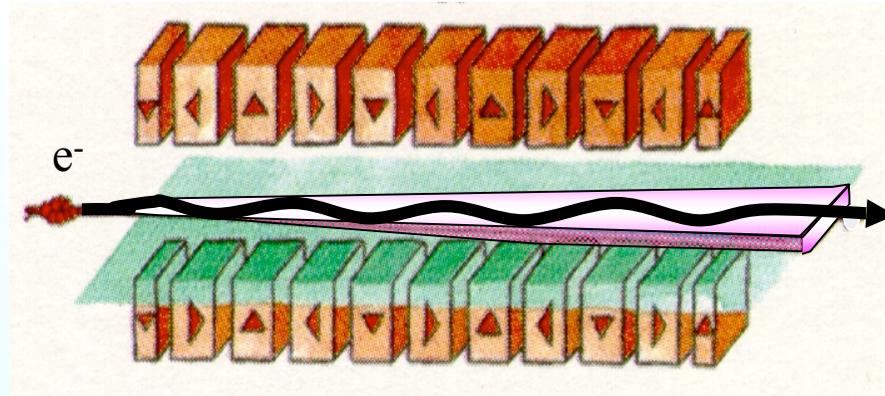
$$Ec = k/R$$

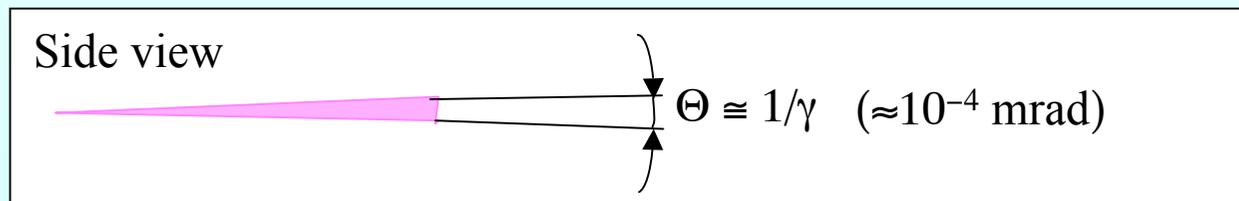
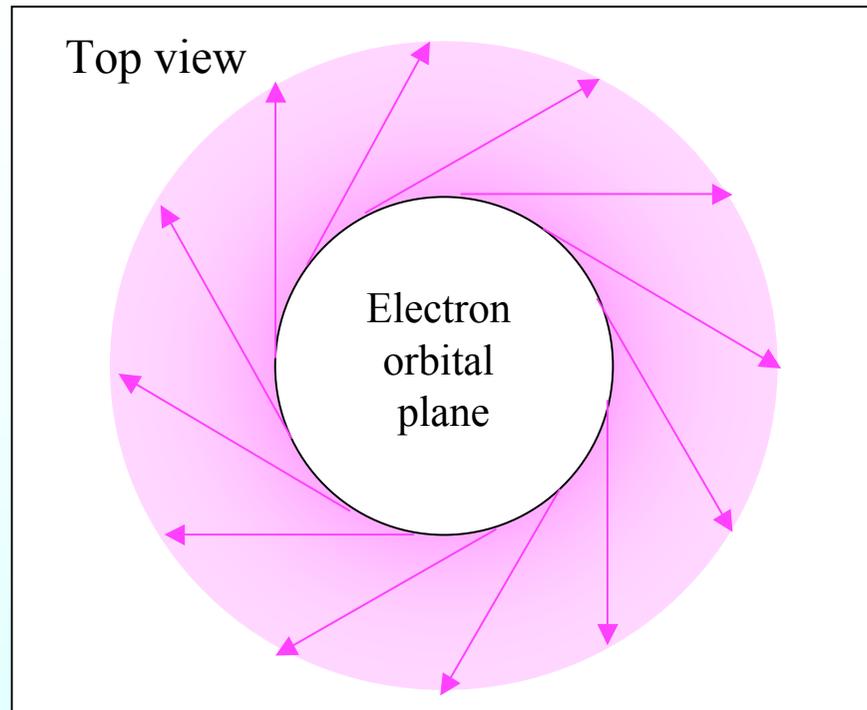


ID comparison

By decreasing the curvature radius of the electron trajectory the spectrum shifts to higher photon energies







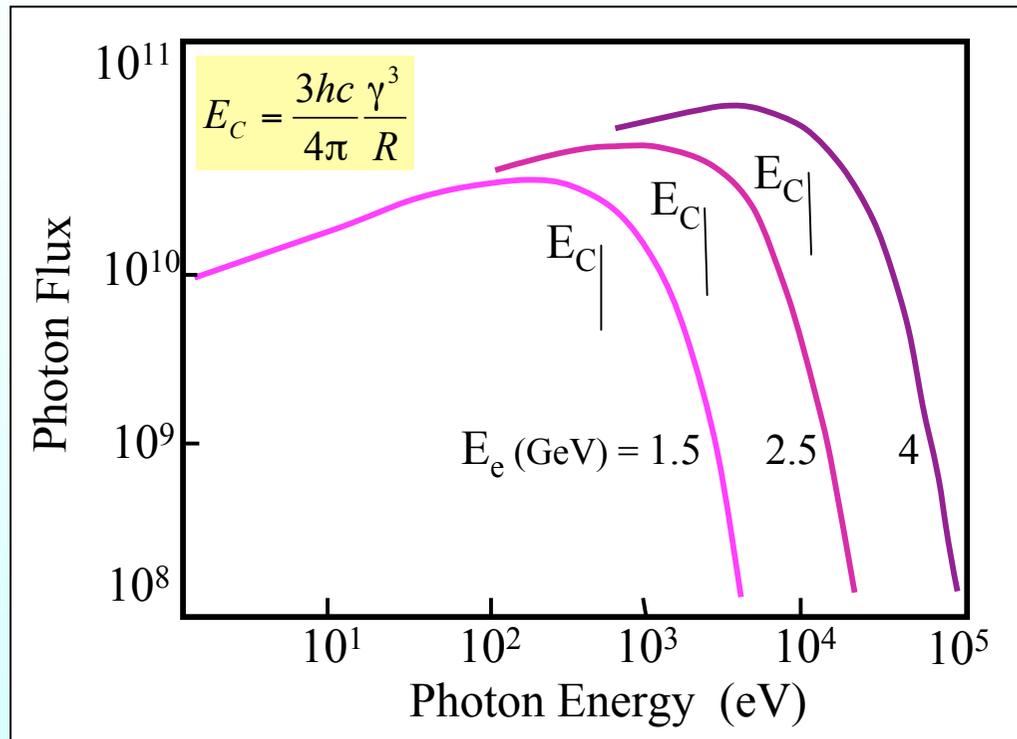
Synchrotron light is spread on the orbital plane as a very thin sheet



Angular distribution



Giuseppe Dalba, University of Trento, Italy

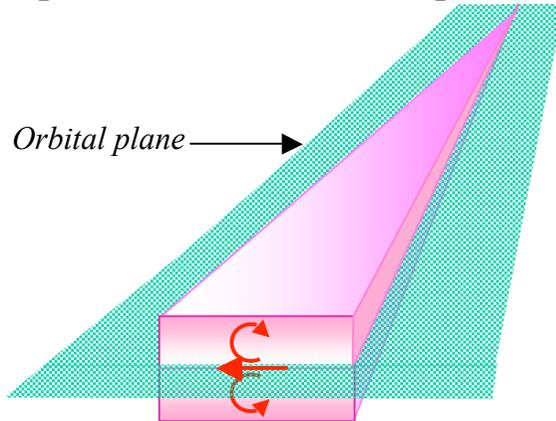


Dependence of the critical photon energy on the electron energy



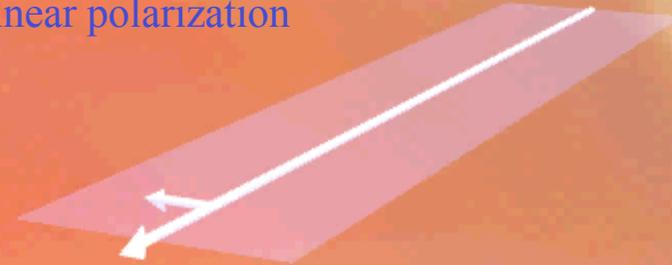
Polarization

The on-axis synchrotron light is polarized in the orbital plane



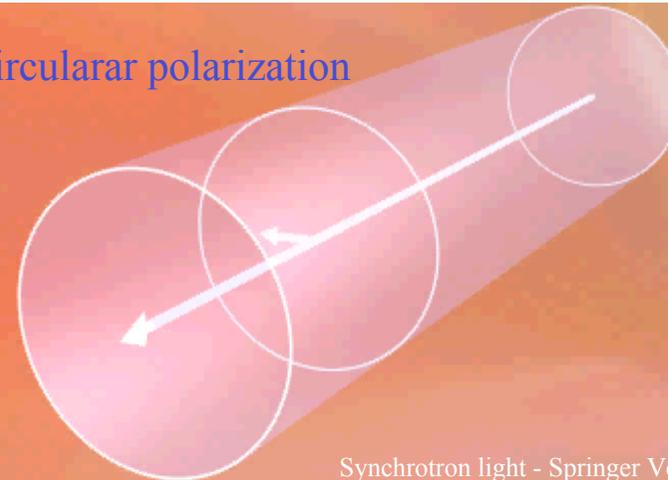
The synchrotron light out of the orbital plane has circular components with opposite helicities above and below the horizontal plane.

Linear polarization



Synchrotron light - Springer Verlag

Circular polarization



Synchrotron light - Springer Verlag

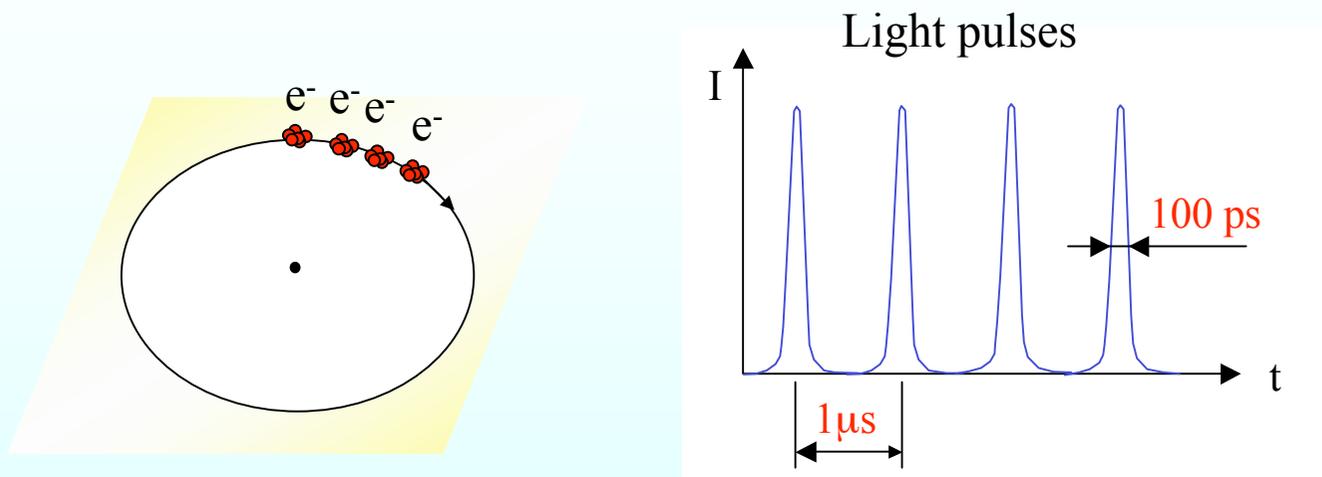
Polarization is exploited for studying magnetic interactions. The difference in absorption in left and right hand circularly polarised light by a solid can be directly related to the ferromagnetic magnetization density (circular dichroism).



Properties



Time structure



Time pulsed emission is interesting for studying rapid reactions

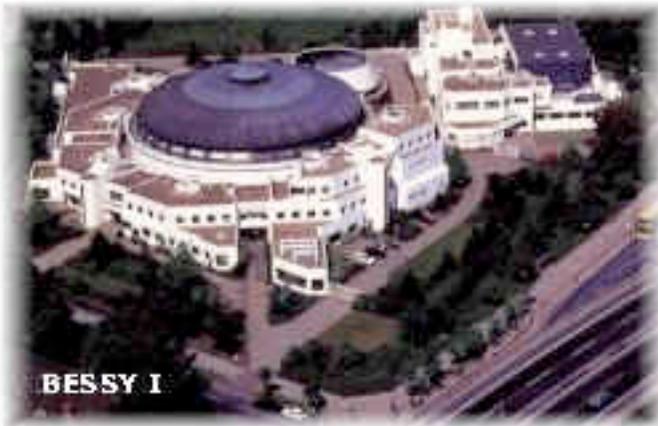
◀ *Properties*



SESAME

Synchrotron-light for Experimental Science and Applications in the Middle East

The SESAME Project aims to establish the Middle East's first major international research center as a cooperative venture by the scientists of the region

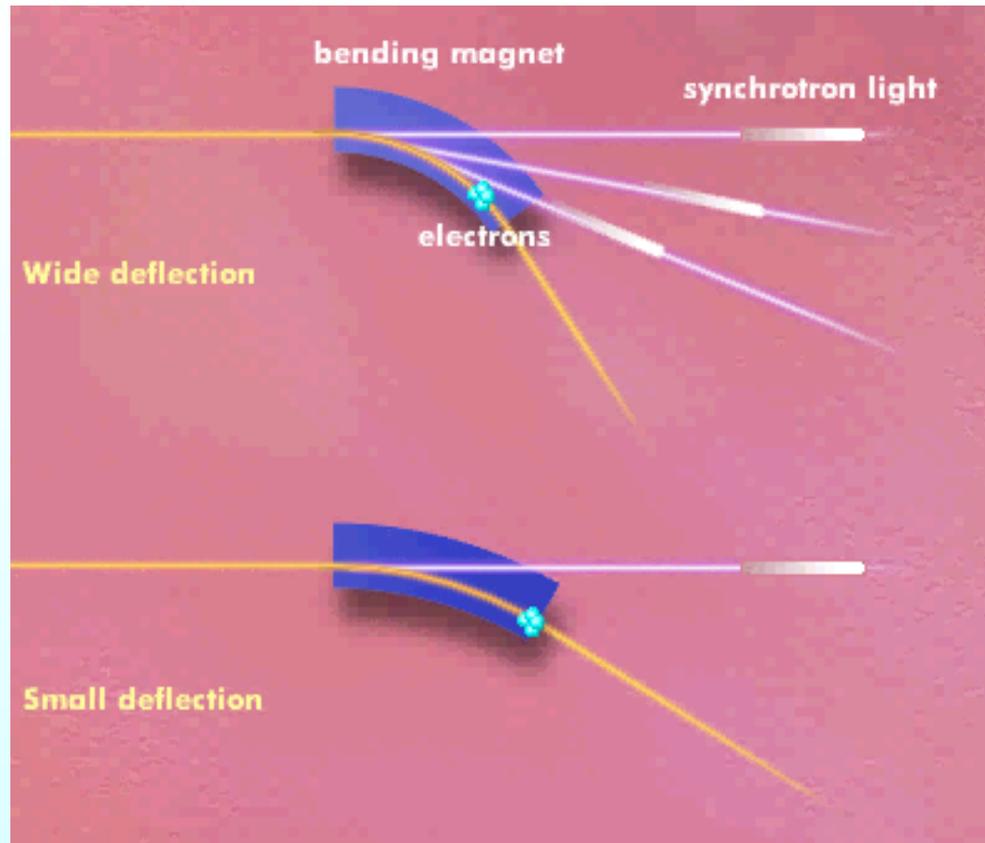


SESAME will have as its centerpiece a synchrotron radiation source based on a gift from Germany of the 0.8 GeV BESSY I storage ring and injector system which stopped operation at the end of November 1999.

Eleven countries have so far joined the project. These are: Armenia, Cyprus, Egypt, Greece, Iran, Israel, Jordan, Morocco, Oman, Palestinian Authority, and Turkey.

The project is being developed under the umbrella of UNESCO and will be located in Allaan, Jordan (30 km from Amman and 30 km from the King Hussein/Allenby Bridge crossing of the Jordan River).



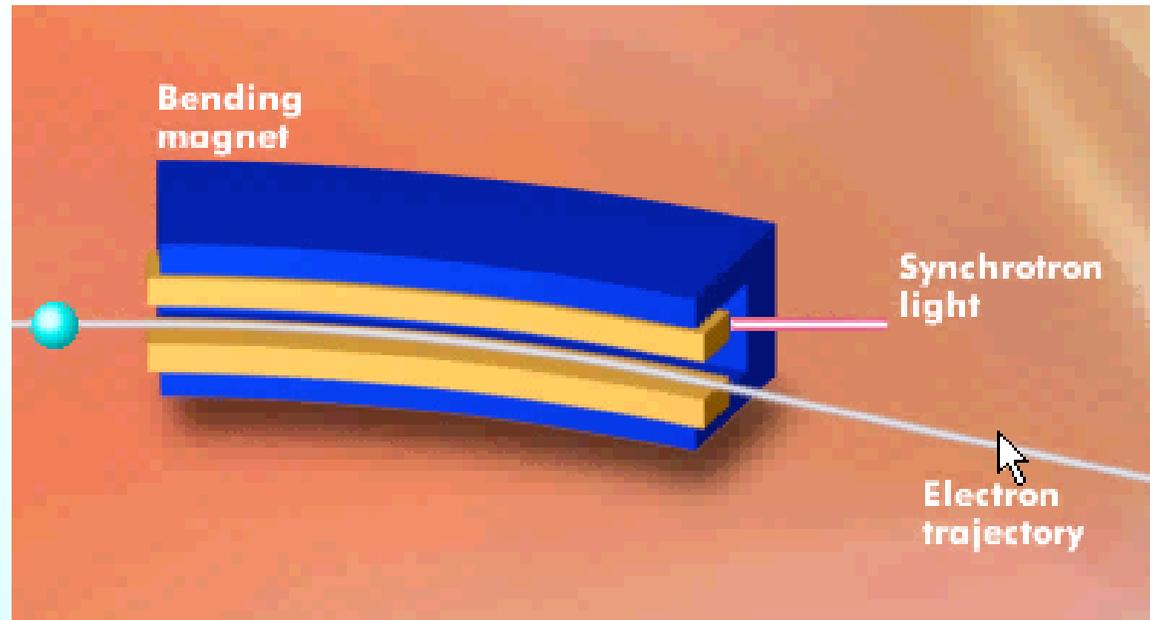


Synchrotron light Springer Verlag

Principle of operation of a bending magnet



Giuseppe Dalba, University of Trento, Italy



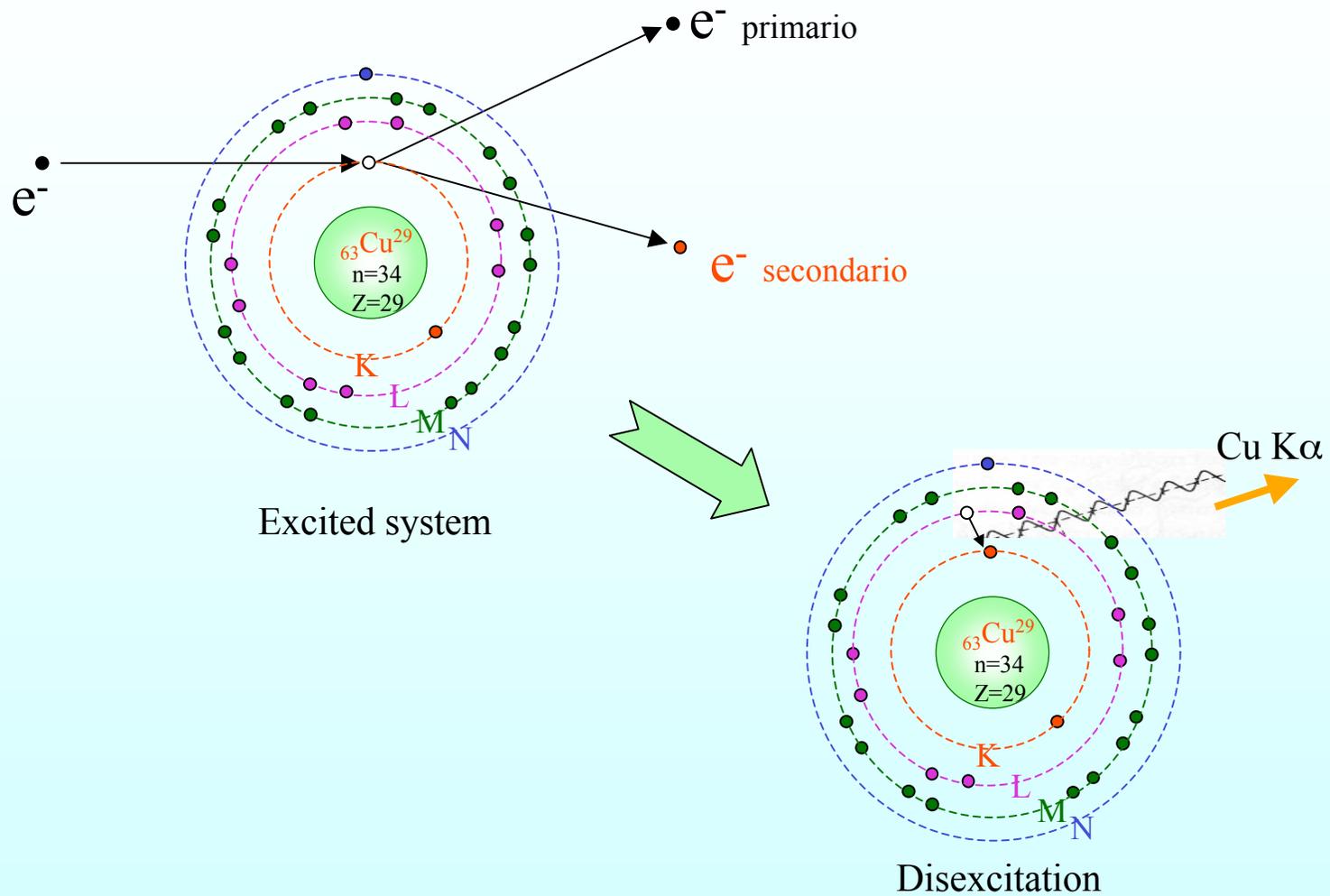
Synchrotron light, Springer-Verlag Compact Disk 2000



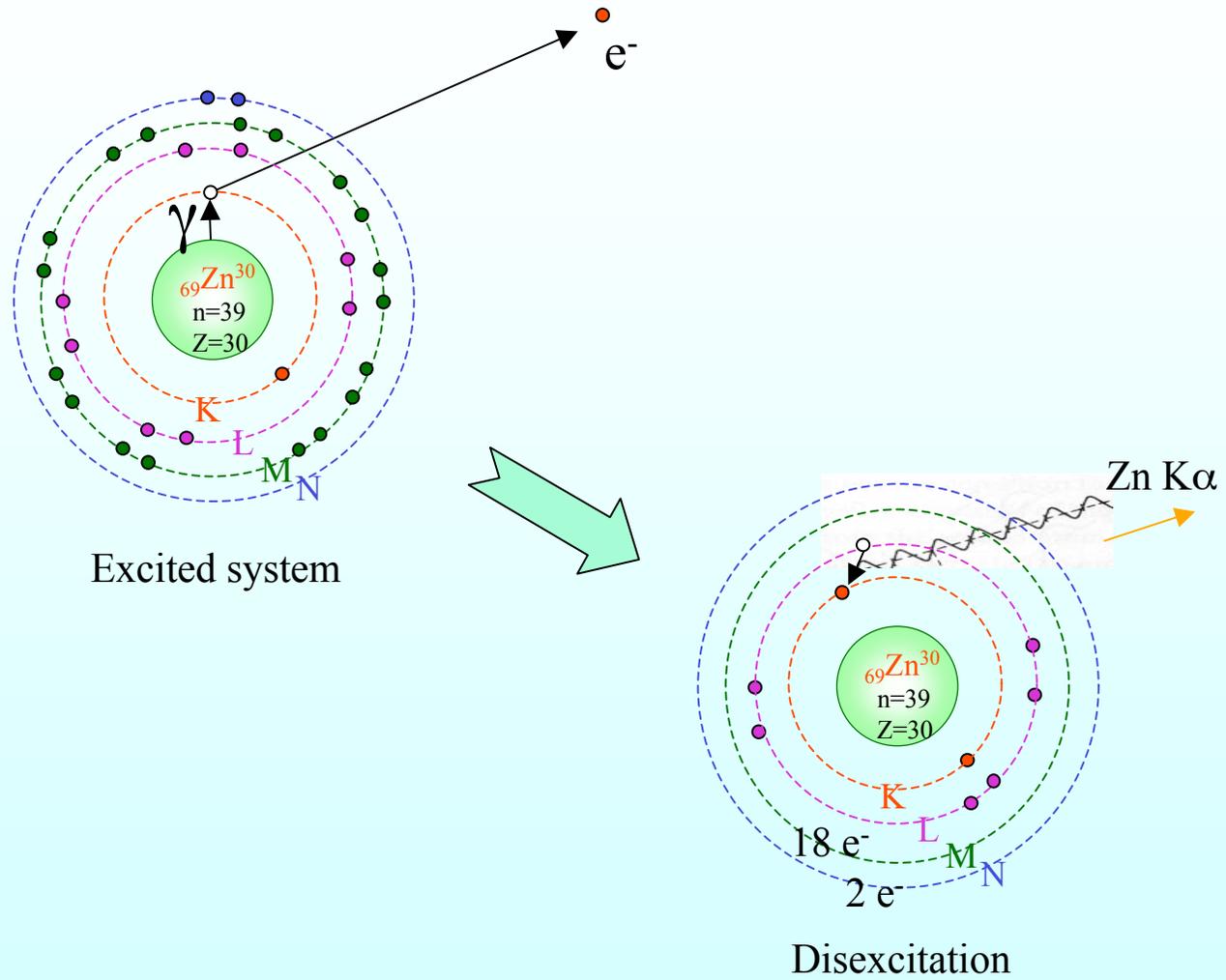
Principle of operation of a bending magnet



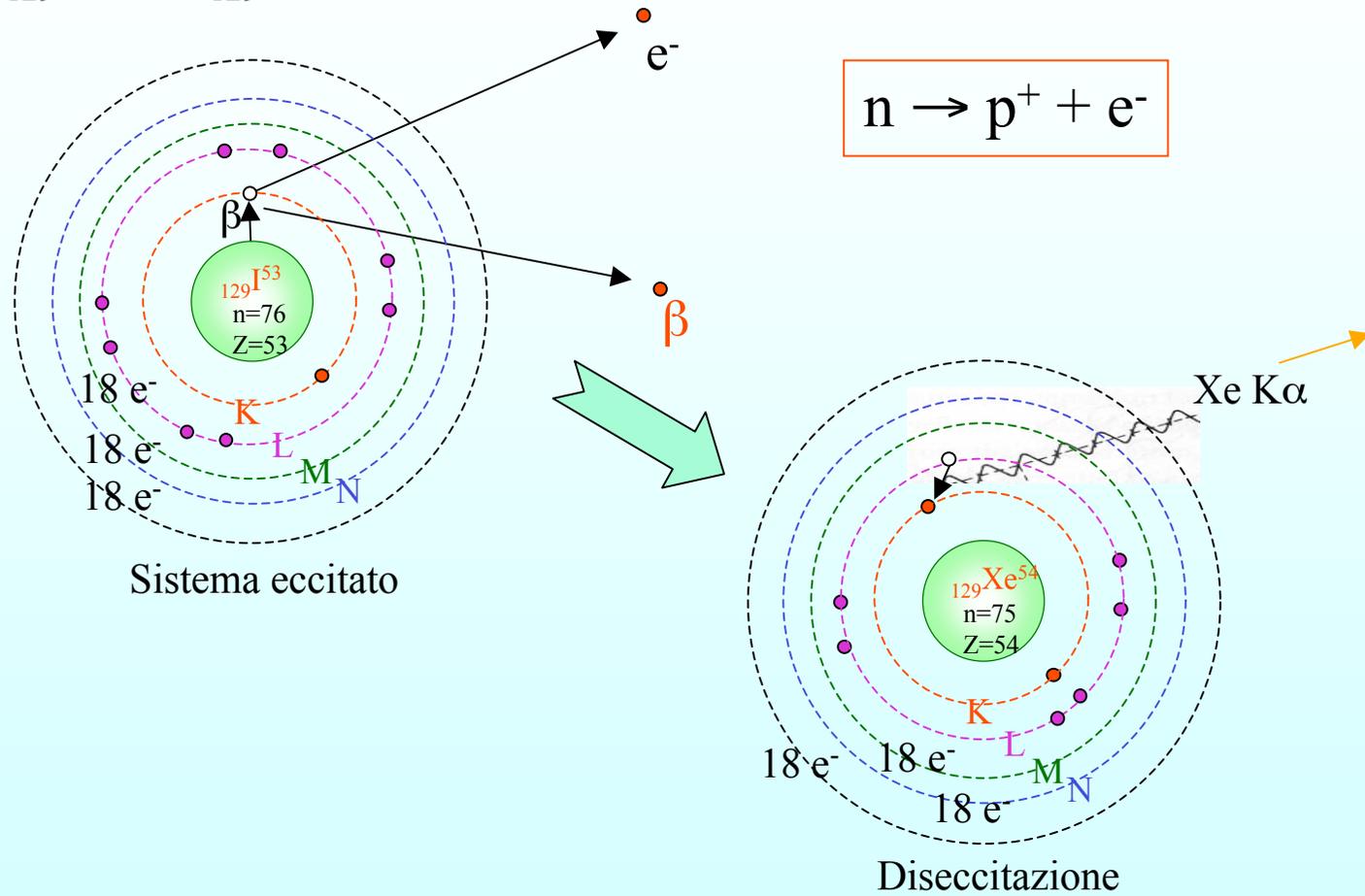
K α excitation



Internal γ conversion



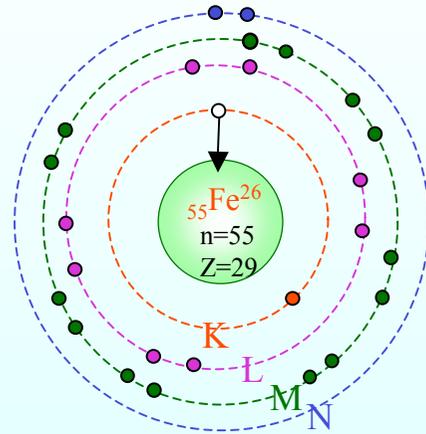
Internal β conversion



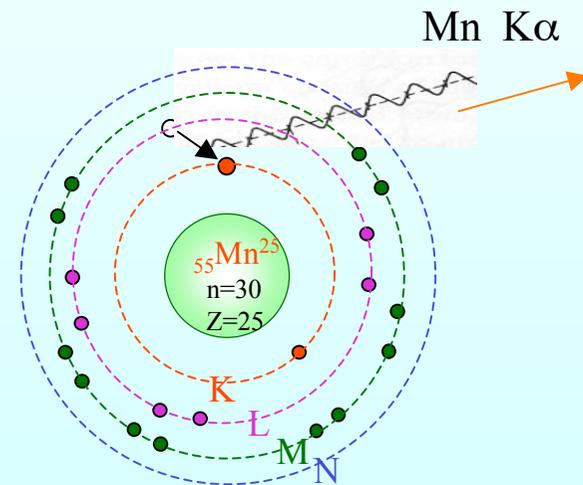
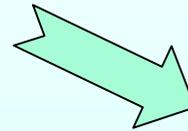
Core electron capture



$$p^+ + e^- \rightarrow n$$



Sistema eccitato



Sistema diseccitato

